Abstract

Language Workbenches offer language designers an expressive environment in which to create their Domain Specific Languages (DSLs). Similarly, research into mechanised meta-theory has shown how dependently typed languages provide expressive environments to formalise and study DSLs and their meta-theoretical properties. But can we claim that dependently typed languages qualify as language workbenches? We argue yes!

We have developed an exemplar DSL called Vélo that showcases not only dependently typed techniques to realise and manipulate Intermediate Representations (IRs), but that dependently typed languages make fine language workbenches. Vélo is a simple verified language with well-typed holes and comes with a complete compiler pipeline: parser, elaborator, REPL, evaluator, and compiler passes. Specifically, we describe our design choices for well-typed IR design that includes support for well-typed holes, how Common Sub-Expression Elimination (CSE) is achieved in a well-typed setting, and how the mechanised type-soundness proof for Vélo is the source of the evaluator.

1 Introduction

Language Workbenches, such as Spoofax [28], offer language designers an expressive environment in which to design, implement, and deploy their Domain Specific Languages (DSLs) [16]. Principally speaking a language workbench [15] is a tool that supports: description of a language’s notation – how we present a language’s concrete syntax to users; implementation of a language’s semantics – how we realise the language’s behaviour; and user interaction through an editor. Outside of these core criteria, various language workbenches support language validation, testing, and composition.
Concurrently, the mechanised meta-theory research programme [7, 1] has seen a wealth of tools and techniques being developed by the programming languages theory community. In particular, dependently typed languages such as Idris 2 [9], Agda [21], and Coq [26] have been widely used to formalise DSLs, and study their meta-theoretical properties. Dependent types allow types to depend on values – that is, types are first class – and provide an expressive environment in which to reason about, and write, our programs. Efforts using dependently typed languages range from studying specific core calculi [4, 24, 10] to building generic reasoning frameworks [25, 3]. These mechanised software verification projects, however, typically stop short of building the frontend that would let users run these verified language implementations. If our verified language implementations type check, we might as well ship them too! By becoming its own implementation language, Idris 2 has successfully demonstrated that this is not an inescapable fate [9]. But can we now claim that dependently typed languages qualify as language workbenches?

Vélo\(^1\) is a minimal functional language that we have realised in Idris 2 to showcase dependently typed techniques to implement and manipulate Intermediate Representations (IRs). This paper introduces Vélo but, most of all, seeks to show that dependently typed languages make fine language workbenches. We address both the core criteria and some optional extensions highlighted by the language workbench challenge [15] for what constitutes a language workbench. Although not all of the optional criteria are met by dependently typed languages, we are convinced that with some additional engineering (taking advantage of existing work, for example Quickchick [18]) more optional criteria can be satisfied.

Another key tenet in language workbenches, such as Spoofax, is the ease with which languages can be created. To that same degree, we have developed a series of reusable modules that captures functionality common to many languages, thereby reducing the boilerplate required when creating Embedded Domain Specific Languages (EDSLs) in Idris 2.

Although we have made an effort to make dependently typed programming accessible in our presentation, more introductory material is available for the interested reader [29, 8].

## 2 Introducing Vélo

The design behind Vélo is purposefully unsurprising: it is the Simply-Typed Lambda Calculus (STLC) extended with let-bindings, booleans and their conjunction, and natural numbers and their addition. To promote the idea of interactive editing Vélo also supports well-typed holes. Below we show an example Vélo program, which contains a multiply used hole, and an extract from the REPL session that lists the current set of holes.

```
let b = false
in let double
    = (fun x : nat => (add x x))
in let x = (double ?hole)
in (double ?hole)
```

Velo> :holes

```
b : Bool
double : Nat -> Nat
----------
?hole : Nat
```

The featherweight language design of Vélo helps us showcase better how we can use dependently typed languages as language workbenches [17]. Regardless of language complexity, Vélo is nonetheless a complete language with a standard compiler pipeline, and REPL. A DSL captures the language’s concrete syntax, and a parser turns DSL instances into raw unchecked terms. Bidirectional type checking keeps type annotations to a minimum in the

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1 A reproducible artifact, and the source code, has been provided as supplementary material.
concrete syntax, and helps to better elaborate raw un-typed terms into a set of well-typed IRs: 
*Holey* to support well-scoped typed holes; and *Terms* the core representation that captures our language’s abstract syntax. We present interesting aspects of our IR design in Section 3. Further, elaboration performs standard desugarings that e.g. turns let-bindings into function application thus reducing the size of our core. From the core representation we also provide well-scoped Common Sub-Expression Elimination (CSE) using co-De Bruijn indexing (Section 4), and we provide a verified evaluator to reduce terms to values (Section 5).

### 3 Language Design

We begin our discussion by detailing the key design rationale on realising the static semantics of Vélo within Idris 2. We have opted to give Vélo an external concrete syntax (a DSL) in which users can write their programs. With dependently typed languages we can also capture the abstract syntax and its static semantics as an intrinsically scoped and typed EDSL directly within the host language [6]. That is to say that the data structure is designed in such a way that we can only represent well scoped and well typed terms and, correspondingly, that our scope- and type- checking passes are guaranteed to have rejected invalid user inputs.

To keep the exposition concise, we focus on a core subset of the language. The interested reader can find the whole definition in the accompanying material.

**Types** are usually introduced using their context free grammar. We present it here on the left-hand side, it gives users the choice between two base types (Nat, and Bool) and a type former for function types (\(\cdot \rightarrow \cdot\)). On the right hand side, we give their internal representation as an inductive type in Idris 2.²

\[
\begin{align*}
t &: \text{TYPE} & \quad \text{data } Ty &= \text{TyNat} \\
& | \quad & \quad & \quad | \quad \text{TyBool} \\
& | \quad & \quad & \quad | \quad \text{TyArr Ty Ty} \\
\end{align*}
\]

**Contexts** can be similarly given by a context free grammar: a context is either empty (\(\varepsilon\)), or an existing context (\(\Gamma\)) extended on the right with a new type assignment (\(x:t\)) using a comma. In Idris 2, we will adopt a nameless representation and so we represent these contexts by using a `SnocList` of types (i.e. lists that grow on the right). Note that the Idris 2 compiler automatically supports sugar for lists and snoc lists: \([1,2,3]\) represents a list counting up from 1 to 3 while \([<1,2,3]\) is its snoc list pendant counting down. In particular \([<]\) denotes the empty snoc list also known as `Lin`.

\[
\begin{align*}
\Gamma &: \text{CONTEXT} & \quad \text{data } \text{SnocList a} &= \text{Lin} \\
& | \quad & \quad & \quad | \quad (\langle<\rangle \text{SnocList a}) a \\
\end{align*}
\]

**Typing Judgements** are given by relations, and encoded in Idris 2 using inductive families, a generalisation of inductive types [14]. Each rule will become a constructor for the family, and so every proof \(\Gamma \vdash t : a\) will correspond to a term \(t\) of type \(\text{Term } \Gamma \ a\). On the left hand side we present two judgements: context membership and a typing judgement, and on the right we have the corresponding inductive family declarations.

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² Throughout this article, the Idris 2 code snippets are automatically rendered using a semantic highlighter. Keywords are typeset in **bold**, types in *blue*, data constructors in *red*, function definitions in *green*, bound variables in **purple**, and comments in *grey.*
Type Theory as a Language Workbench

\[ \Gamma \ni x : a \quad \text{data} \quad \text{Elem} : (\gamma : \text{SnocList} \ \text{ty}) \rightarrow (a : \text{ty}) \rightarrow \text{Type} \]

\[ \Gamma \vdash t : a \quad \text{data} \quad \text{Term} : (\gamma : \text{SnocList} \ \text{Ty}) \rightarrow (a : \text{Ty}) \rightarrow \text{Type} \]

We leave the definition of \text{Elem} to the next section, focusing instead on \text{Term}. The most basic of typing rules are axioms, they have no premise and are mapped to constructors with no argument. We use \text{Idris} 2 comments (\text{--}) to format our constructor’s type in such a way that they resemble the corresponding inference rule. Here we show the rule stating that 0 is a natural number and its translation as the \text{Zero} constructor.

\[ \text{Var} : \quad \text{Elem} \ \gamma \ a \rightarrow \quad \underline{------------------} \quad \text{Term} \ \gamma \ a \]

Next, we have typing rules with a single premise which is not a subderivation of the relation itself. They are mapped to constructors with a single argument. Here we show the typing rule for variables: given a proof that we have a variable of type \( a \) somewhere in the context, we can build a term of type \( a \) in said context.

\[ \text{Inc} : \quad \text{Term} \ \gamma \ \text{TyNat} \rightarrow \quad \underline{------------------} \quad \text{Term} \ \gamma \ \text{TyNat} \]

Similarly, rules with two premises are translated to constructors with two arguments, one for each subderivation. Here we present the typing rule for application nodes: provided that the function has a function type, and the argument has a type matching the function’s domain, the application has a type corresponding to the function’s codomain. Note that the context \( \Gamma \) is the same across the whole rule and so the same \( \gamma \) is used everywhere.

\[ \text{App} : \quad \text{Term} \ \gamma \ (\text{TyArr} \ a \ b) \rightarrow \quad \underline{------------------------} \quad \text{Term} \ \gamma \ b \]

Finally, we have a rule where the premise’s context has been extended: a function of type \( (a \rightarrow b) \) is built by providing a term of type \( b \) defined in a context extended with a new variable of type \( a \).

\[ \text{Func} : \quad \text{Term} \ (\gamma :< a) \ b \rightarrow \quad \underline{------------------------} \quad \text{Term} \ \gamma \ (\text{TyArr} \ a \ b) \]
Using this intrinsically typed representation, we can readily represent entire typing derivations. The following example presents the internal representation Plus2 of the derivation proving that \((\lambda x \cdot (\text{Inc} (\text{Inc} x)))\) can be assigned the type \((\text{Nat} \rightarrow \text{Nat})\).

\[
\begin{align*}
\epsilon, x : \text{Nat} &\vdash (\text{Inc} (\text{Inc} x)) : \text{Nat} \\
\epsilon \vdash (\lambda x \cdot (\text{Inc} (\text{Inc} x))) : \text{Nat} \rightarrow \text{Nat}
\end{align*}
\]

By using Term as an IR in our compiler we have made entire classes of invalid programs unrepresentable: it is impossible to form an ill scoped or ill typed term. Indeed, trying to write an ill scoped or an ill typed program leads to a static error as demonstrated by the following failing blocks. In this first example we try to refer to a variable in an empty context. Idris 2 correctly complains that this is not possible.

\[
\text{failing "Mismatch between: ?gamma :< TyNat and [<]."}
\]

\[
\begin{align*}
\text{Ouch} & : \text{Term} [\langle] \text{TyNat} \\
\text{Ouch} & = \text{Var} \text{Here}
\end{align*}
\]

In this second example we try to type the identity function as a function from \text{Nat} to \text{Bool}. This is statically rejected as nonsensical: \text{TyNat} and \text{TyBool} are distinct constructors!

\[
\text{failing "Mismatch between: TyBool and TyNat."}
\]

\[
\begin{align*}
\text{Ouch} & : \text{Term} [\langle] \text{TyArr TyNat TyBool} \\
\text{Ouch} & = \text{Func} \ (\text{Var} \text{Here})
\end{align*}
\]

Using such intrinsically typed EDSLs we can statically enforce that our elaborators do check that the raw terms obtained by parsing user input are well scoped and well typed. Writing our compiler passes (model-to-model transformations) and evaluation engine (model-to-host transformation) using these invariant-rich IRs additionally ensures that each step respects the language’s static semantics. In fact we will describe in Section 5 how we can use our EDSLs to both verify our static semantics whilst describing our dynamic semantics.

For languages equipped with more advanced type systems, that cannot be as easily enforced statically, we can retain some of these guarantees by using a well scoped core language rather than a well typed one. This is the approach used in Idris 2 and it has already helped eliminate an entire class of bugs arising when attempting to solve a metavariable with a term that was defined in a different context [9].

### 3.1 Efficient De Bruijn Representation

A common strategy for implementing well-scoped terms is to use typed De Bruijn indices [13], which are easily realised as an inductive family [14] indicating where in the type-level context the variable is bound.

Concretely, we index the \text{Elem} family by a context (once again represented as a \text{SnocList} of kinds) and the kind of the variable it represents.

\[
\Gamma \ni x : a \\
data \text{Elem} : (\text{gamma} : \text{SnocList} \text{ty}) \rightarrow (a : \text{ty}) \rightarrow \text{Type}
\]

\text{Here} will be defined in Section 3.1 as a constructor for the \text{Elem} family.

Idris 2 only accepts failing blocks if checking their content yields an error matching the given string.
We then match each context membership inference rule to a constructor. The **Here** constructor indicates that the variable of interest is the most local one in scope (note the non-linear occurrence of \((x : a)\) on the left hand side, and correspondingly of \(ty\) on the right).

\[
\Gamma, x : a \ni x : a \\
\text{Here :} \quad \text{----------------------} \\
\text{Elem (gamma :< ty) ty}
\]

The **There** constructor skips past the most local variable to look for the variable of interest deeper in the context.

\[
\Gamma \ni x : a \\
\Gamma, y : b \ni x : a \\
\text{There :} \quad \text{----------------------} \\
\text{Elem (gamma :< _) ty}
\]

Whilst a valid definition, this approach unfortunately does not scale to large contexts: every **Elem** proof is linear in the size of the De Bruijn index that it represents. To improve the runtime efficiency of the representation we instead opt to model De Bruijn indices as natural numbers, which Idris 2 compiles to GMP-style unbounded integers. Further, we need to additionally define an **AtIndex** family to ensure that all of the natural numbers we use correspond to valid indices. We pointedly reuse the **Elem** names because these **Here** and **There** constructors play exactly the same role.

```
data AtIndex : (ty : kind) -> (ctxt : SnocList kind) -> (idx : Nat) -> Type where
  Here : AtIndex ty (ctxt :< ty) 0
  There : AtIndex ty ctxt idx -> AtIndex ty (ctxt :< _) (1 + idx)
```

We then define a variable as the pairing of a natural number and an erased (as indicated by the 0 annotation on the binding site for \(prf\)) proof that the given natural number is indeed a valid De Bruijn index.

```
data IsVar : (ctxt : SnocList kind) -> (ty : kind) -> Type where
  V : (idx : Nat) -> (0 prf : AtIndex ty ctxt idx) -> IsVar ctxt ty
```

Thanks to Quantitative Type Theory [19, 5] as implemented in Idris 2, the compiler knows that it can safely erase these runtime-irrelevant proofs. we now have the best of both worlds: a well-scoped realisation of De Bruijn indices that is compiled efficiently.

Just like the naïve definition of De Bruijn indexing is not the best suited for a practical implementation, the inductive family **Term** described in Section 3 is not the most convenient to use. We will now see one of its limitations and how we remedied it in Vélo.

### 3.2 Compact Constant Folding

Software Foundations’ *Programming Language Foundations* opens with a constant-folding transformation exercise [23, Chapter 1]. Starting from a small language of expressions (containing natural numbers, variables, addition, subtraction, and multiplication) we are to deploy the semiring properties to simplify expressions. The definition of the simplifying traversal contains much duplicated code due to the way the source language is structured: all the binary operations are separate constructors, whose subterms need to be structurally simplified before we can decide whether a rule applies. The correction proof has just as much duplication because it needs to follow the structure of the call graph of the function it wants to see reduced. The only saving grace here is that Coq’s tactics language lets users write scripts that apply to many similar goals thus avoiding duplication in the source file.
In Vélo, we structure our core language’s representation in an algebraic manner so that this duplication is never needed. All builtin operators (from primitive operations on builtin types to function application itself) are represented using a single \texttt{Call} constructor which takes an operation and a type-indexed list of subterms.

\begin{verbatim}
data Term : (ctxt : SnocList Ty) -> Ty -> Type where Var : IsVar ctxt ty -> Term ctxt ty Fun : Term (ctxt :< a) b -> Term ctxt (TyArr a b) Call : {tys : _} -> (operator : Prim tys ty) -> (operands : Terms ctxt tys) -> Term ctxt ty
\end{verbatim}

Here \texttt{Terms} is the pointwise lifting of \texttt{Term} to lists of types. In practice we use the generic \texttt{All} quantifier, but this is morally equivalent to the specialised version presented below:

\begin{verbatim}
data Terms : (ctxt : SnocList Ty) -> List Ty -> Type where Nil : Terms ctxt Nil (::) : Term ctxt ty -> Terms ctxt tys -> Terms ctxt (ty :: tys)
\end{verbatim}

The primitive operations can now be enumerated in a single datatype \texttt{Prim} which lists the primitive operation’s arguments and the associated return type.

\begin{verbatim}
\end{verbatim}

Using \texttt{Prim}, structural operations can now be implemented by handling recursive calls on the subterms of \texttt{Call} nodes uniformly before dispatching on the operator to see whether additional simplifications can be deployed. Similarly, all of the duplication in the correction proofs is factored out in a single place where the induction hypotheses can be invoked.

### 3.3 Well-Typed Holes

Holes are a special kind of placeholder that programmers can use for parts of the program they have not yet written. In a typed language, each hole will be assigned a type based on the context it is used in.

\textit{Type-Driven Development} [22] is a practice by which the user enters into a dialogue with the compiler to interactively build the program. We can enable type-driven programming in part by providing special language support for holes and operations on them. Such operations will include the ability to inspect, refine, compute with, and instantiate (with an adequately typed term) holes. We believe that bare-bones language support for type-driven development should at least include the ability to: (1) inspect the type of a hole and the local context it appears in; (2) instantiate a hole with an adequately typed term; and as well (3) safely evaluate programs that still contain holes. Vélo provides all three.

Idris 2 elaborates holes as it encounters them by turning them into global declarations with no associated definition. Because of this design choice users cannot mention the same hole explicitly in different places to state their intention that these yet unwritten terms ought to be the same. Users can refer to the hole’s solution by its name, but that hole is placed in one specific position and it is from that position that Idris 2 infers its context.
In Vélo, however, we allow holes to be mentioned arbitrarily many times in arbitrarily different local contexts. In the following example, the hole \(?h\) occurs in two distinct contexts: \(\varepsilon, a, x\) and \(\varepsilon, a, y\).

\[
\lambda a. \ \lambda x. \ ^{?h} \ \lambda y. \ ^{?h}
\]

As a consequence, a term will only fit in that hole if it happens to live in the shared common prefix of these two contexts \((\varepsilon, a)\). Indeed, references to \(x\) will not make sense in \(\varepsilon, a, y\) and vice-versa for \(y\).

Our elaborator proceeds in two steps. First, a bottom-up pass records holes as they are found and, in nodes with multiple subterms, reconciles conflicting hole occurrences by computing the appropriate local context restrictions. This process produces a list of holes, their types, and local contexts, together with a Holey term that contains invariants ensuring these collected holes do fit in the term. Second, a top-down pass produces a core Term indexed by the list of Meta (a simple record type containing the hole’s name, the context it lives in, and its type). Hole occurrences end up being assigned a thinning that embeds the metavariable’s actual context into the context it appears in. We discuss thinnings and their use in Vélo in Section 4.

Although these intermediate representations are Vélo-specific, the technique and invariants are general and can be reused by anyone wanting to implement well-scoped holes in their functional DSL.

### 4 Compiler Passes

Now that our core language is well-scoped by construction, our compiler passes must also be shown to be scope-preserving. This is not a new requirement, merely it makes concrete a constraint that used to be enforced informally. More importantly we show, with our compiler passes, that model-to-same-model transformation of our EDSL is possible, and that the infrastructure required is not bespoke to Vélo.

The purpose of CSE is to identify subterms that appear multiple times in the syntax tree, and to abstract over them to avoid needless recomputations at runtime. In the following example for instance, we would like to let-bind \(t\) before the application node (denoted \(\$\)) so that \(t\) may be shared by both subtrees.

\[
\$ \ \lambda x. \ \lambda a. \ t \ \lambda b. \ t
\]

One of the challenges of CSE, as exemplified above, is that the term of interest may be buried deep inside separate contexts. In our intrinsically scoped representation, \(t\) in scope \(\Gamma, x : \sigma\) is potentially not actually syntactically equal to a copy living in \(\Gamma, a : \tau, b : \nu\). Indeed a variable \(v\) bound in \(\Gamma\) will, for instance, be represented by the De Bruijn index \((1 + v)\) in \(\Gamma, x : \sigma\) but by the index \((2 + v)\) in \(\Gamma, a : \tau, b : \nu\).
If only terms were indexed by their exact support (i.e. a context restricted to the variables actually used in the term)! We would not care about additional yet irrelevant variables that happen to be in scope. The principled solution here is to switch to a different representation when performing CSE. The co-De Bruijn representation [20] provides exactly this guarantee.

In the co-De Bruijn representation, every term is precisely indexed by its exact support. That is to say that every subterm explicitly throws away the bound variables that are not mentioned in it. By the time we reach a variable node, a single bound variable remains in scope: precisely the one being referred to.

This process of throwing unused variables away is reified using thinnings i.e. renamings that are injective, and order preserving. We can think of thinnings as sequences of 0/1 bits, stating whether each variable is kept or dropped.

Below, we give a graphical presentation (taken from [2]) of the $S$ combinator (the lambda term $\lambda g. \lambda f. \lambda x. g(x)(f(x))$) in co-De Bruijn notation. In it we represent thinnings (i.e. lists of bits) as lists of either $\bullet$ (1) or $\circ$ (0).

The first three $\lambda$ abstractions only use $\bullet$ in their thinnings because all of $g$, $f$, and $x$ do appear in the body of the combinator. The first application node then splits the context into two: the first subterm ($gx$) drops $f$ while the second ($fx$) gets rid of $g$. Further application nodes select the one variable still in scope for each leaf subterm: $g$, $x$, $f$, and $x$.

Using a co-De Bruijn representation, we can identify shared subterms: they need to not be mentioning any of the most local variables and be syntactically equal. Our pass successfully transforms the program on the left-hand side to the one on the right-hand side where the repeated expressions $(\text{add } m \ n)$ and $(\text{add } n \ m)$ have been let-bound.

```
let m = zero in
let n = (inc zero) in
in (add (add (add m n) (add n m))
    (add (add m n) (add m n)))
```

```
let m = zero in
let n = (inc zero) in
let p = (add n m) in
let q = (add m n) in
in (add (add q p) (add p q))
```

This pass relies on the ability to have a compact representation of thinnings (as the co-De Bruijn representation makes heavy use of them), and additionally the existence of a cheap equality test for them. This is not the case in the implementation we include in Vélo but it is a solved problem [2].

5 Execution

The Vélo REPL lets users reduce terms down to head-normal forms. We can realise Vélo’s dynamic semantics either through definitional interpreters [4, 6], or by providing a more traditional syntactic proof of type-soundness [30] but mechanised [29, Part 2: Properties] using inductive families.
We chose the latter approach: by using inductive families, we can make explicit our language’s operational semantics. This enables us to study its meta-theoretical properties and in particular prove a progress result: every term is either a value or can take a reduction step. By repeatedly applying the progress result, until we either reach a value or the end user runs out of patience and kills the process, this proof freely gives us an evaluator that is guaranteed to be correct with respect to Vélo’s operational semantics.

Following existing approaches [29, Part 2: Properties], we have defined inductive families describing how terms reduce.

```agda
data Redux : (this, that : Term ctxt type) -> Type where
  SimplifyCall : (op : Prim tys ty)
    -> (step : Reduxes these those)
    -> Redux (Call p these) (Call p those)

  ReduceFuncApp : {body : Term (ctxt :, type) return}
    -> {arg : Term ctxt type}
    -> {value : Value arg}
    -> Redux (Call App [Fun body, arg])
    (subst arg body)
```

As can be seen above, our setting enforces call-by-value: as described by the rule ReduceFuncApp \( (\lambda(x) \cdot b) t \) only reduces to \( b \{x \leftarrow t \} \) if \( t \) is already known to be a value. Furthermore, our algebraic design (Section 3.2) allows us to easily enforce a left-to-right evaluation order by having a generic family describing how primitive operations’ arguments reduce. As can be seen below: when considering a type-aligned list of arguments, either the head takes a step and the rest is unchanged, or the head is already known to be a value and a further argument is therefore allowed to take a step.

```agda
data Reduxes : (these, those : Terms ctxt tys) -> Type where
  (!:) : (hd : Redux this that)
    -> (rest : Terms ctxt tys)
    -> Reduxes (this :: rest) (that :: rest)

  (::) : (value : Value hd)
    -> (tl : Reduxes these those)
    -> Reduxes (hd :: these) (hd :: those)
```

We differ, however, from standard approaches by making our proofs of progress generic such that the boilerplate for computing the reflexive transitive closure when reducing terms is tidied away in a shareable module. Our top-level progress definition is thus parameterised by reduction and value definitions:

```agda
data Progress : (0 value : Pred a) -> (0 redux : Rel a) -> (tm : a) -> Type
  where Done : {0 tm : a} -> (val : value tm) -> Progress value redux tm

  Step : {this, that : a}
    -> (step : redux this that) -> Progress value redux this
```

and the result of execution, which is similarly parameterised, is as follows (where RTList is the type taking a relation and returning its reflexive-transitive closure):
data Result : (value : Pred a) -> (0 redux : Rel a) -> (this : a) -> Type
where R : (that : a) -> (val : value that)
    -> (steps : RTList redux this that) -> Result value redux this

The benefit of our approach is that language designers need only provide details of what
reductions are, and how to compute a single reduction, the rest comes for free. Moreover,
with the result of evaluation we also get the list of reduction steps made that can, optionally,
be printed to show a trace of execution.

6 Conclusion

We have shown that dependently typed languages satisfy the core requirements from the
Language Workbench Challenge [15]. Vélo’s notation as a DSL is, by design, textual, and
the internal core bounded by Idris 2’s own notation requirements. More importantly the
semantics (statics and dynamics) of Vélo are verified as part of the implementation thanks
to the dependently typed setting. The weakest supported core criteria, unfortunately, is that
for editor support. Languages created through Idris 2 do not get an editor, they are free
form languages which require their parsers and elaborators be hand written. This can change
with future investigation. Idris 2 has support for elaborator reflection [11] which provides a
vehicle through which deriving parsers and elaborators can happen.

There are, however, more criteria from the language workbench feature model to consider:
semantic & syntactic services for editors; testing & debugging; and composability.

With the rise of the Language Server Protocol (LSP) it would be a good idea to look
at how we can derive LSP compatible language servers generically, thus addressing the
missing provision of the optional semantic and syntactic services. Idris 2 itself provides an
IDE-Protocol, and there is support for the LSP in Idris 2.

Our languages also do not come with the ability to test and debug their implementation.
Some of the features we have presented are fully formalised (e.g. execution), others are only
known to be scope-and-type preserving (e.g. CSE). Therefore the dependently typed setting
does not mean we do not need testing anymore. Prior work on generators for inductive
families [18] should allow us to bring property-based testing [12] to our core passes.

Finally there is language composability. It would be advantageous to support the reuse of
existing languages, and their type-systems when designing new ones. This is a hard problem:
One has to not only combine their semantics but also the remainder of the workbench tooling.
The language fragments approach [27] provides a solution to language composability for
intrinsically typed definitional interpreters, but this does not extend to workbench tooling.
Extending this approach to our definition of semantics based on inductive families and to
creating composable workbench tooling is an open problem.

We strongly believe that with future engineering we can satisfy these missing criteria,
and make dependently typed languages a mighty fine language workbench.

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