

# Repetitions in Strings: A “Constant” Problem

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## Abstract

Repeating structures in strings is one of the most fundamental characteristics of strings, and has been an important topic in the field of combinatorics on words and combinatorial pattern matching since their beginnings. In this talk, I will focus on squares and maximal repetitions and review the “runs” theorem [1] as well as related results (e.g. [5, 6, 7, 3, 2, 4]) which address the two main questions: how many of them can be contained in a string of given length, and algorithms for computing them.

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