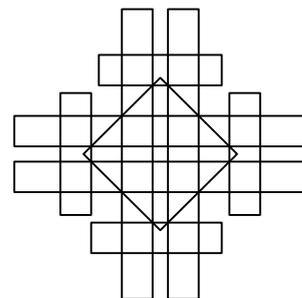


# 40th International Symposium on Computational Geometry

SoCG 2024, June 11-14, 2024, Athens, Greece

Edited by

Wolfgang Mulzer  
Jeff M. Phillips



*Editors*

**Wolfgang Mulzer** 

Freie Universität Berlin, Germany  
mulzer@inf.fu-berlin.de

**Jeff M. Phillips** 

University of Utah, USA  
jeffp@cs.utah.edu

*ACM Classification 2012*

Theory of computation → Computational geometry; Theory of computation → Design and analysis of algorithms; Mathematics of computing → Combinatorics; Mathematics of computing → Graph algorithms

**ISBN 978-3-95977-316-4**

*Published online and open access by*

Schloss Dagstuhl – Leibniz-Zentrum für Informatik GmbH, Dagstuhl Publishing, Saarbrücken/Wadern, Germany. Online available at <https://www.dagstuhl.de/dagpub/978-3-95977-316-4>.

*Publication date*

June, 2024

*Bibliographic information published by the Deutsche Nationalbibliothek*

The Deutsche Nationalbibliothek lists this publication in the Deutsche Nationalbibliografie; detailed bibliographic data are available in the Internet at <https://portal.dnb.de>.

*License*

This work is licensed under a Creative Commons Attribution 4.0 International license (CC-BY 4.0): <https://creativecommons.org/licenses/by/4.0/legalcode>.



In brief, this license authorizes each and everybody to share (to copy, distribute and transmit) the work under the following conditions, without impairing or restricting the authors' moral rights:

- Attribution: The work must be attributed to its authors.

The copyright is retained by the corresponding authors.

Digital Object Identifier: 10.4230/LIPIcs.SoCG.2024.0

ISBN 978-3-95977-316-4

ISSN 1868-8969

<https://www.dagstuhl.de/lipics>

## LIPICs – Leibniz International Proceedings in Informatics

LIPICs is a series of high-quality conference proceedings across all fields in informatics. LIPICs volumes are published according to the principle of Open Access, i.e., they are available online and free of charge.

### *Editorial Board*

- Luca Aceto (Reykjavik University, IS and Gran Sasso Science Institute, IT)
- Christel Baier (TU Dresden, DE)
- Roberto Di Cosmo (Inria and Université de Paris, FR)
- Faith Ellen (University of Toronto, CA)
- Javier Esparza (TU München, DE)
- Daniel Král' (Masaryk University, Brno, CZ)
- Meena Mahajan (*Chair*, Institute of Mathematical Sciences, Chennai, IN)
- Anca Muscholl (University of Bordeaux, FR)
- Chih-Hao Luke Ong (University of Oxford, GB)
- Phillip Rogaway (University of California, Davis, US)
- Eva Rotenberg (Technical University of Denmark, Lyngby, DK)
- Raimund Seidel (Universität des Saarlandes, Saarbrücken, DE and Schloss Dagstuhl – Leibniz-Zentrum für Informatik, Wadern, DE)
- Pierre Senellart (ENS, Université PSL, Paris, FR)

**ISSN 1868-8969**

**<https://www.dagstuhl.de/lipics>**



# ■ Contents

Preface	
<i>Wolfgang Mulzer and Jeff M. Phillips</i> .....	0:xi
Conference Organization	
.....	0:xiii
Additional Reviewers	
.....	0:xvii

## Regular Papers

A Universal In-Place Reconfiguration Algorithm for Sliding Cube-Shaped Robots in a Quadratic Number of Moves	
<i>Zachary Abel, Hugo A. Akitaya, Scott Duke Kominers, Matias Korman, and     Frederick Stock</i> .....	1:1–1:14
Clustering with Few Disks to Minimize the Sum of Radii	
<i>Mikkel Abrahamsen, Sarita de Berg, Lucas Meijer, André Nusser, and     Leonidas Theocharous</i> .....	2:1–2:15
On the Number of Digons in Arrangements of Pairwise Intersecting Circles	
<i>Eyal Ackerman, Gábor Damásdi, Balázs Keszegh, Rom Pinchasi, and     Rebeka Raffay</i> .....	3:1–3:14
Semi-Algebraic Off-Line Range Searching and Biclique Partitions in the Plane	
<i>Pankaj K. Agarwal, Esther Ezra, and Micha Sharir</i> .....	4:1–4:15
Communication Complexity and Discrepancy of Halfplanes	
<i>Manasseh Ahmed, Tsun-Ming Cheung, Hamed Hatami, and Kusha Sareen</i> .....	5:1–5:17
Probabilistic Analysis of Multiparameter Persistence Decompositions into Intervals	
<i>Ángel Javier Alonso, Michael Kerber, and Primoz Skraba</i> .....	6:1–6:19
ETH-Tight Algorithm for Cycle Packing on Unit Disk Graphs	
<i>Shinwoo An and Eunjin Oh</i> .....	7:1–7:15
Eight-Partitioning Points in 3D, and Efficiently Too	
<i>Boris Aronov, Abdul Basit, Indu Ramesh, Gianluca Tasinato, and Uli Wagner</i> ...	8:1–8:15
A Clique-Based Separator for Intersection Graphs of Geodesic Disks in $\mathbb{R}^2$	
<i>Boris Aronov, Mark de Berg, and Leonidas Theocharous</i> .....	9:1–9:15
Discrete Fréchet Distance Oracles	
<i>Boris Aronov, Tsuru Farhana, Matthew J. Katz, and Indu Ramesh</i> .....	10:1–10:14
Tight Bounds for the Learning of Homotopy à la Niyogi, Smale, and Weinberger for Subsets of Euclidean Spaces and of Riemannian Manifolds	
<i>Dominique Attali, Hana Dal Poz Kouřimská, Christopher Fillmore, Ishika Ghosh,     André Lieutier, Elizabeth Stephenson, and Mathijs Wintraecken</i> .....	11:1–11:19



An $O(n \log n)$ -Time Approximation Scheme for Geometric Many-To-Many Matching <i>Sayan Bandyopadhyay and Jie Xue</i> .....	12:1–12:15
Topological $k$ -Metrics <i>Willow Barkan, Huck Bennett, and Amir Nayyeri</i> .....	13:1–13:13
Totally Geodesic Surfaces in Hyperbolic 3-Manifolds: Algorithms and Examples <i>Brannon Basilio, Chaeryn Lee, and Joseph Malionek</i> .....	14:1–14:19
Wrapping Cycles in Delaunay Complexes: Bridging Persistent Homology and Discrete Morse Theory <i>Ulrich Bauer and Fabian Roll</i> .....	15:1–15:16
A Coreset for Approximate Furthest-Neighbor Queries in a Simple Polygon <i>Mark de Berg and Leonidas Theodoropoulos</i> .....	16:1–16:16
Towards Space Efficient Two-Point Shortest Path Queries in a Polygonal Domain <i>Sarita de Berg, Tillmann Miltzow, and Frank Staals</i> .....	17:1–17:16
Plane Hamiltonian Cycles in Convex Drawings <i>Helena Bergold, Stefan Felsner, Meghana M. Reddy, Joachim Orthaber, and Manfred Scheucher</i> .....	18:1–18:16
Fully Dynamic Maximum Independent Sets of Disks in Polylogarithmic Update Time <i>Sujoy Bhore, Martin Nöllenburg, Csaba D. Tóth, and Jules Wolms</i> .....	19:1–19:16
Constrained and Ordered Level Planarity Parameterized by the Number of Levels <i>Václav Blažej, Boris Klemz, Felix Klesen, Marie Diana Sieper, Alexander Wolff, and Johannes Zink</i> .....	20:1–20:16
On Edge Collapse of Random Simplicial Complexes <i>Jean-Daniel Boissonnat, Kunal Dutta, Soumik Dutta, and Siddharth Pritam</i> .....	21:1–21:16
Reconfiguration of Plane Trees in Convex Geometric Graphs <i>Nicolas Bousquet, Lucas de Meyer, Théo Pierron, and Alexandra Wesolek</i> .....	22:1–22:17
A Canonical Tree Decomposition for Chirotopes <i>Mathilde Bouvel, Valentin Feray, Xavier Goaoc, and Florent Koechlin</i> .....	23:1–23:18
Dynamic Convex Hulls for Simple Paths <i>Bruce Brewer, Gerth Stølting Brodal, and Haitao Wang</i> .....	24:1–24:15
Fine-Grained Complexity of Earth Mover’s Distance Under Translation <i>Karl Bringmann, Frank Staals, Karol Węgrzycki, and Geert van Wordragen</i> .....	25:1–25:17
Approximating the Geometric Knapsack Problem in Near-Linear Time and Dynamically <i>Moritz Buchem, Paul Deuker, and Andreas Wiese</i> .....	26:1–26:14
Map-Matching Queries Under Fréchet Distance on Low-Density Spanners <i>Kevin Buchin, Maike Buchin, Joachim Gudmundsson, Aleksandr Popov, and Sampson Wong</i> .....	27:1–27:15
Computing Shortest Closed Curves on Non-Orientable Surfaces <i>Denys Bulavka, Éric Colin de Verdière, and Niloufar Fuladi</i> .....	28:1–28:16

Practical Software for Triangulating and Simplifying 4-Manifolds <i>Rhuidi Antonio Burke</i> .....	29:1–29:23
Effective Computation of the Heegaard Genus of 3-Manifolds <i>Benjamin A. Burton and Finn Thompson</i> .....	30:1–30:16
Geometric Matching and Bottleneck Problems <i>Sergio Cabello, Siu-Wing Cheng, Otfried Cheong, and Christian Knauer</i> .....	31:1–31:15
SCARST: Schnyder Compact and Regularity Sensitive Triangulation Data Structure <i>Luca Castelli Aleardi and Olivier Devillers</i> .....	32:1–32:19
Semialgebraic Range Stabbing, Ray Shooting, and Intersection Counting in the Plane <i>Timothy M. Chan, Pingan Cheng, and Da Wei Zheng</i> .....	33:1–33:15
Convex Polygon Containment: Improving Quadratic to Near Linear Time <i>Timothy M. Chan and Isaac M. Hair</i> .....	34:1–34:15
Enclosing Points with Geometric Objects <i>Timothy M. Chan, Qizheng He, and Jie Xue</i> .....	35:1–35:15
Dynamic Geometric Connectivity in the Plane with Constant Query Time <i>Timothy M. Chan and Zhengcheng Huang</i> .....	36:1–36:13
Optimal Euclidean Tree Covers <i>Hsien-Chih Chang, Jonathan Conroy, Hung Le, Lazar Milenković, Shay Solomon, and Cuong Than</i> .....	37:1–37:15
Computing Diameter+2 in Truly-Subquadratic Time for Unit-Disk Graphs <i>Hsien-Chih Chang, Jie Gao, and Hung Le</i> .....	38:1–38:14
Nearly Orthogonal Sets over Finite Fields <i>Dror Chawin and Ishay Haviv</i> .....	39:1–39:11
Optimal Algorithm for the Planar Two-Center Problem <i>Kyungjin Cho, Eunjin Oh, Haitao Wang, and Jie Xue</i> .....	40:1–40:15
GPU Algorithm for Enumerating PL Spheres of Picard Number 4: Application to Toric Topology <i>Suyoung Choi, Hyeontae Jang, and Mathieu Vallée</i> .....	41:1–41:15
Fast Approximations and Coresets for $(k, \ell)$ -Median Under Dynamic Time Warping <i>Jacobus Conradi, Benedikt Kolbe, Ioannis Psarros, and Dennis Rohde</i> .....	42:1–42:17
An Improved Lower Bound on the Number of Pseudoline Arrangements <i>Fernando Cortés Kühnast, Justin Dallant, Stefan Felsner, and Manfred Scheucher</i> .....	43:1–43:18
Stability and Approximations for Decorated Reeb Spaces <i>Justin Curry, Washington Mio, Tom Needham, Osman Berat Okutan, and Florian Russold</i> .....	44:1–44:17
Sweeping Arrangements of Non-Piercing Regions in the Plane <i>Suryendu Dalal, Rahul Gangopadhyay, Rajiv Raman, and Saurabh Ray</i> .....	45:1–45:15

Saturation Results Around the Erdős–Szekeres Problem <i>Gábor Damásdi, Zichao Dong, Manfred Scheucher, and Ji Zeng</i> .....	46:1–46:14
Robustly Guarding Polygons <i>Rathish Das, Omrit Filtser, Matthew J. Katz, and Joseph S.B. Mitchell</i> .....	47:1–47:17
Hopf Arborescent Links, Minor Theory, and Decidability of the Genus Defect <i>Pierre Dehornoy, Corentin Lunel, and Arnaud de Mesmay</i> .....	48:1–48:18
Computing Zigzag Vineyard Efficiently Including Expansions and Contractions <i>Tamal K. Dey and Tao Hou</i> .....	49:1–49:15
Cup Product Persistence and Its Efficient Computation <i>Tamal K. Dey and Abhishek Rathod</i> .....	50:1–50:15
Efficient Algorithms for Complexes of Persistence Modules with Applications <i>Tamal K. Dey, Florian Russold, and Shreyas N. Samaga</i> .....	51:1–51:18
Colorful Intersections and Tverberg Partitions <i>Michael Gene Dobbins, Andreas F. Holmsen, and Dohyeon Lee</i> .....	52:1–52:13
Maximum Betti Numbers of Čech Complexes <i>Herbert Edelsbrunner and János Pach</i> .....	53:1–53:14
An Improved Bound on Sums of Square Roots via the Subspace Theorem <i>Friedrich Eisenbrand, Matthieu Haeberle, and Neta Singer</i> .....	54:1–54:8
Dimensionality of Hamming Metrics and Rademacher Type <i>Alexandros Eskenazis</i> .....	55:1–55:13
Light, Reliable Spanners <i>Arnold Filtser, Yuval Gitlitz, and Ofer Neiman</i> .....	56:1–56:15
Multicut Problems in Embedded Graphs: The Dependency of Complexity on the Demand Pattern <i>Jacob Focke, Florian Hörsch, Shaohua Li, and Dániel Marx</i> .....	57:1–57:15
Fréchet Edit Distance <i>Emily Fox, Amir Nayyeri, Jonathan James Perry, and Benjamin Raichel</i> .....	58:1–58:15
A Structure Theorem for Pseudo-Segments and Its Applications <i>Jacob Fox, János Pach, and Andrew Suk</i> .....	59:1–59:14
Near Optimal Locality Sensitive Orderings in Euclidean Space <i>Zhimeng Gao and Sariel Har-Peled</i> .....	60:1–60:14
Approximating the Maximum Independent Set of Convex Polygons with a Bounded Number of Directions <i>Fabrizio Grandoni, Edin Husić, Mathieu Mari, and Antoine Tinguely</i> .....	61:1–61:16
Approximating Multiplicatively Weighted Voronoi Diagrams: Efficient Construction with Linear Size <i>Joachim Gudmundsson, Martin P. Seybold, and Sampson Wong</i> .....	62:1–62:14
Faster Fréchet Distance Approximation Through Truncated Smoothing <i>Thijs van der Horst and Tim Ophelders</i> .....	63:1–63:15

Moderate Dimension Reduction for $k$ -Center Clustering <i>Shaofeng H.-C. Jiang, Robert Krauthgamer, and Shay Sapir</i> .....	64:1–64:16
On the Parameterized Complexity of Motion Planning for Rectangular Robots <i>Iyad Kanj and Salman Parsa</i> .....	65:1–65:15
Zarankiewicz’s Problem via $\epsilon$ -t-Nets <i>Chaya Keller and Shakhar Smorodinsky</i> .....	66:1–66:15
Separator Theorem and Algorithms for Planar Hyperbolic Graphs <i>Sándor Kisfaludi-Bak, Jana Masaříková, Erik Jan van Leeuwen, Bartosz Walczak, and Karol Węgrzycki</i> .....	67:1–67:17
A Quadtree, a Steiner Spanner, and Approximate Nearest Neighbours in Hyperbolic Space <i>Sándor Kisfaludi-Bak and Geert van Wordragen</i> .....	68:1–68:15
The Medial Axis of Any Closed Bounded Set Is Lipschitz Stable with Respect to the Hausdorff Distance Under Ambient Diffeomorphisms <i>Hana Dal Poz Kouřimská, André Lieutier, and Mathijs Wintraecken</i> .....	69:1–69:18
Strange Random Topology of the Circle <i>Uzu Lim</i> .....	70:1–70:17
Beyond Chromatic Threshold via $(p, q)$ -Theorem, and Blow-Up Phenomenon <i>Hong Liu, Chong Shangguan, Jozef Skokan, and Zixiang Xu</i> .....	71:1–71:15
A 1.9999-Approximation Algorithm for Vertex Cover on String Graphs <i>Daniel Lokshantov, Fahad Panolan, Saket Saurabh, Jie Xue, and Meirav Zehavi</i> ..	72:1–72:11
Demystifying Latschev’s Theorem: Manifold Reconstruction from Noisy Data <i>Sushovan Majhi</i> .....	73:1–73:16
Polychromatic Colorings of Geometric Hypergraphs via Shallow Hitting Sets <i>Tim Planken and Torsten Ueckerdt</i> .....	74:1–74:14
Morse Theory for the $k$ -NN Distance Function <i>Yohai Reani and Omer Bobrowski</i> .....	75:1–75:16
Grid Peeling of Parabolas <i>Günter Rote, Moritz Rüber, and Morteza Saghaian</i> .....	76:1–76:18
A Topological Version of Schaefer’s Dichotomy Theorem <i>Patrick Schneider and Simon Weber</i> .....	77:1–77:16
Pach’s Animal Problem Within the Bounding Box <i>Martin Tancer</i> .....	78:1–78:18
Algorithms for Halfplane Coverage and Related Problems <i>Haitao Wang and Jie Xue</i> .....	79:1–79:15
Measure-Theoretic Reeb Graphs and Reeb Spaces <i>Qingsong Wang, Guanqun Ma, Raghavendra Sridharamurthy, and Bei Wang</i> .....	80:1–80:18
Faster Approximation Scheme for Euclidean $k$ -TSP <i>Ernest van Wijland and Hang Zhou</i> .....	81:1–81:12
Space Complexity of Euclidean Clustering <i>Xiaoyi Zhu, Yuxiang Tian, Lingxiao Huang, and Zengfeng Huang</i> .....	82:1–82:16

**CG Challenge**

Computing Maximum Polygonal Packings in Convex Polygons Using Best-Fit, Genetic Algorithms and ILPs <i>Alkan Atak, Kevin Buchin, Mart Hagedoorn, Jona Heinrichs, Karsten Hogreve, Guangping Li, and Patrick Pawelczyk</i> .....	83:1–83:9
Shadoks Approach to Knapsack Polygonal Packing <i>Guilherme D. da Fonseca and Yan Gerard</i> .....	84:1–84:9
Priority-Driven Nesting of Irregular Polygonal Shapes Within a Convex Polygonal Container Based on a Hierarchical Integer Grid <i>Martin Held</i> .....	85:1–85:6
A General Heuristic Approach for Maximum Polygon Packing <i>Canhui Luo, Zhouxing Su, and Zhipeng Lü</i> .....	86:1–86:9

**Media Expositions**

The Ultimate Frontier: An Optimality Construction for Homotopy Inference <i>Dominique Attali, Hana Dal Poz Kouřimská, Christopher Fillmore, Ishika Ghosh, André Lieutier, Elizabeth Stephenson, and Mathijs Wintraecken</i> .....	87:1–87:6
Computational Geometry Concept Videos: A Dual-Use Project in Education and Outreach <i>Marjolein Haagsman, Maarten Löffler, and Carola Wenk</i> .....	88:1–88:4
Optimal In-Place Compaction of Sliding Cubes <i>Irina Kostitsyna, Tim Ophelders, Irene Parada, Tom Peters, Willem Sonke, and Bettina Speckmann</i> .....	89:1–89:4
Visualizing Lucas’s Hamiltonian Paths Through the Associahedron 1-Skeleton <i>Kacey Thien-Huu La, Jose E. Arbelo, and Christopher J. Tralie</i> .....	90:1–90:6
Image Triangulation Using the Sobel Operator for Vertex Selection <i>Olivia X. Laske and Lori Ziegelmeier</i> .....	91:1–91:7
Ipelets for the Convex Polygonal Geometry <i>Nithin Parepally, Ainesh Chatterjee, Auguste H. Gezalayan, Hongyang Du, Sukrit Mangla, Kenny Wu, Sarah Hwang, and David M. Mount</i> .....	92:1–92:7

## ■ Preface

The 40th International Symposium on Computational Geometry (SoCG 2024) was held at the Eugenides Foundation in Athens, Greece, June 11–14, 2024, as part of the Computational Geometry Week (CG Week 2024).

The conference received a record 235 submissions, and after a thorough review process, in which each paper was evaluated by three or more independent reviewers, the program committee accepted 82 papers for presentation. Two submissions were merged into a single paper for presentation. These proceedings contain extended abstracts of the accepted papers, limited to 500 lines (excluding references). If any supporting material does not fit in the line limit, the full paper is available at a public repository and referenced in the corresponding extended abstract.

The **Best Paper Award** of SoCG 2024 went to the paper “An  $O(n \log n)$ -Time Approximation Scheme for Geometric Many-to-Many Matching” by Sayan Bandyopadhyay and Jie Xue; this paper has been invited to submit an extended version to the Journal of the ACM. The **Best Student Paper Award** of SoCG 2024 went to the paper “Practical Software for Triangulating and Simplifying 4-Manifolds” by Rhuaidi Burke. This was the first year bestowing a best student paper award; all authors of the paper needed to be students at time of submission (or very recently graduated) to be eligible. The **Best Student Presentation Award** was determined and announced at the symposium, based on ballots cast by the attendees. For the first time, a paper was selected for submission to the newly-established diamond open access journal TheoretCS: “Optimal Algorithm for the Planar Two-Center Problem” by Kyungjin Chu, Eunjin Oh, Haitao Wang, and Jie Xue. Additionally, a selection of papers was invited to submit an extended version to forthcoming special issues of Discrete & Computational Geometry and the Journal of Computational Geometry dedicated to the symposium.

The **SoCG Test of Time Awards** of this year go to “Surface Reconstruction by Voronoi Filtering” by Nina Amenta and Marshall W. Bern, which was published in SoCG 1998, and to “A Pivoting Algorithm for Convex Hulls and Vertex Enumeration of Arrangements and Polyhedra” by David Avis and Komei Fukuda, which was published in SoCG 1991.

The scientific program of CG Week 2024 was enriched by two distinguished invited speakers. An invited talk, entitled “The Particle and Wave Theories of Shape”, was given by Leonidas J. Guibas from Stanford University. A second invited talk, entitled “Sketching Techniques for Metric Data”, was delivered by Edith Cohen from Google Research and Tel Aviv University. We thank the plenary speakers for kindly accepting our invitation.

In addition to the technical papers, there were six submissions to the multimedia exposition. Submissions were reviewed and six of them were accepted for presentation. The extended abstracts that describe these submissions are included in this proceedings volume. The multimedia content can be found at <https://www.computational-geometry.org>.

The 6th Computational Geometry Challenge was part of CG Week 2024. The challenge problem was to pack as many polygons from a provided set inside of a given convex polygon. This year, there were nine teams participating in the challenge, and these proceedings contain contributions by the four top-placed teams describing their winning approaches.

We thank the authors of all submitted works. We are most grateful to the members of the SoCG Program Committee, the Media Exposition Committee, and the CG Challenge Committee for their dedication, expertise, and hard work that ensured the high quality of



the works in these proceedings. We are grateful for the assistance provided by the hundreds of reviewers; without their help, it would have been nearly impossible to run the selection process. Finally, we thank Philipp Kindermann for meticulous work as Proceedings Chair.

Many other people contributed to the success of SoCG 2024 and the entire CG Week. We are very grateful to the local organization committee for their work in organizing the event. Finally, we thank all the members of the Test of Time Award, Workshop, and Young Researchers Forum Committees, the CG Challenge Advisory Board, and the Computational Geometry Steering Committee.

- Wolfgang Mulzer  
SoCG Program Committee Co-Chair  
Freie Universität Berlin
- Jeff M. Phillips  
SoCG Program Committee Co-Chair  
University of Utah

## ■ Conference Organization

### SoCG Program Committee

- Peyman Afshani (Aarhus University, Denmark)
- Hee-Kap Ahn (Pohang University of Science and Technology, South Korea)
- Boris Aronov (New York University, USA)
- Sayan Bandyapadhyay (Portland State University, USA)
- Gill Barequet (Technion - Israel Inst. of Technology, Israel)
- Karl Bringmann (Universität des Saarlandes, Germany)
- Maike Buchin (Ruhr-Universität Bochum, Germany)
- Tamal Dey (Purdue University, USA)
- Omrit Filtser (Open University of Israel, Israel)
- Sariel Har-Peled (University of Illinois, Urbana-Champaign, USA)
- Meng He (Dalhousie University, Canada)
- Michael Hoffmann (Eidgenössische Technische Hochschule Zürich, Switzerland)
- Chaya Keller (Ariel University, Israel)
- Clement Maria (INRIA, France)
- David Mount (University of Maryland, USA)
- Wolfgang Mulzer (co-chair; Freie Universität Berlin, Germany)
- Steve Oudot (INRIA, France)
- Dömötör Pálvölgyi (Eötvös Loránd University, Hungary)
- Evanthia Papadopoulou (Università della Svizzera italiana, Switzerland)
- Salman Parsa (DePaul University, USA)
- Zuzana Patáková (Univerzita Karlova, Czech Republic)
- Jeff M. Phillips (co-chair; University of Utah, USA)
- Benjamin Raichel (University of Texas at Dallas, USA)
- Lena Schlipf (University of Tübingen, Germany)
- Melanie Schmidt (Heinrich Heine University Düsseldorf, Germany)
- Micha Sharir (Tel Aviv University, Israel)
- Rodrigo Silveira (Universitat Politècnica de Catalunya, Spain)
- Andrew Suk (University of California, San Diego, USA)
- Subhash Suri (University of California, Santa Barbara, USA)
- Martin Tancer (Univerzita Karlova, Czech Republic)
- Yufei Tao (The Chinese University of Hong Kong, China)
- Csaba D. Tóth (California State University Northridge, USA)
- Birgit Vogtenhuber (Technische Universität Graz, Austria)

### SoCG Proceedings Chair

- Philipp Kindermann (Universität Trier)

40th International Symposium on Computational Geometry (SoCG 2024).

Editors: Wolfgang Mulzer and Jeff M. Phillips



Leibniz International Proceedings in Informatics

Schloss Dagstuhl – Leibniz-Zentrum für Informatik, Dagstuhl Publishing, Germany



### **Media Exposure Committee**

- Kevin Buchin (TU Dortmund, Germany)
- Siu-Wing Cheng (HKUST - Kowloon, Hong Kong)
- Barbara Giunti (University of Albany, USA)
- Michał Lipiński (Institute of Mathematics, Polish Academy of Sciences, Poland)
- Talha bin Masood (Linköping University, Sweden)
- Alexander McCleary (Ohio State University, USA)
- Abhishek Rathod (Ben Gurion University, Israel)
- Raghavendra Sridharamurthy (co-chair; University of Utah, USA)
- Anastasios Stefanou (University of Bremen, Germany)
- Bei Wang (chair; University of Utah, USA)
- Carola Wenk (Tulane University, USA)

### **CG Challenge Committee**

- Sándor Fekete (TU Braunschweig, DE)
- Phillip Keldenich (TU Braunschweig, DE)
- Dominik Krupke (TU Braunschweig, DE)
- Stefan Schirra (Universität Magdeburg)

### **CG Challenge Advisory Board**

- Bill Cook (University of Waterloo)
- Andreas Fabri (Geometry Factory)
- Dan Halperin (Tel Aviv University)
- Michael Kerber (TU Graz)
- Philipp Kindermann (Universität Trier)
- Joe Mitchell (Stony Brook University, US)
- Kevin Verbeek (TU Eindhoven)

### **SoCG Test of Time Award Committee**

- Pankaj K. Agarwal (Duke University)
- Siu-Wing Cheng (HKUST)
- Raimund Seidel (Saarland University)

### **Workshop Committee**

- Anne Driemel (University of Bonn, DE)
- Sándor Fekete (TU Braunschweig, DE)
- Matya Katz (Ben-Gurion University, IL)
- Marc van Kreveld (Utrecht University, NL)
- Joe Mitchell (Stony Brook University, US)
- Yusu Wang (University of California, San Diego, US)

### Young Researchers Forum Program Committee

- Elena Arseneva (Università della Svizzera italiana, Switzerland)
- Omrit Filtser (Open University of Israel, Israel)
- Mayank Goswami (CUNY Queens College, USA)
- Irina Kostitsyna (KBR at NASA Ames Research Center, USA)
- Erik Krohn (University of Wisconsin, USA)
- Yakov Nekrich (Michigan Technological University, USA)
- Valentin Polishchuk (chair; Linköping University, Sweden)
- Frank Staals (Utrecht University, the Netherlands)
- Csaba D. Tóth (California State University Northridge, USA)
- Mikael Vejdemo-Johansson (CUNY College of Staten Island, USA)
- Kevin Verbeek (TU Eindhoven, the Netherlands)

### Local Organizing Committee

- Ioannis Emiris (chair; Athena Research Center & University of Athens, Greece)
- Georgios Alexis Ioannakis (Athena Research Center, Greece)
- Evanthia Papadopoulou (Università della Svizzera italiana, Switzerland)
- Ioannis Psarros (Archimedes, Athena Research Center, Greece)
- Eleni Sotiropoulou (Athena Research Center, Greece)
- Konstantinos Tsakalidis (University of Liverpool, UK)

### Steering Committee (2022–2024)

- Anne Driemel (University of Bonn, DE)
- Sándor Fekete (TU Braunschweig, DE)
- Matya Katz (Ben-Gurion University, IL)
- Marc van Kreveld (Utrecht University, NL)
- Joe Mitchell (Stony Brook University, US)
- Yusu Wang (University of California, San Diego, US)



## ■ Additional Reviewers

Ahmed Abdelkader  
Mikkel Abrahamsen  
Aditya Acharya  
Eyal Ackerman  
Henry Adams  
Pankaj K. Agarwal  
Péter Ágoston  
Taehoon Ahn  
Bernhard K. Aichernig  
Oswin Aichholzer  
Elad Aigner-Horev  
Hugo Akitaya  
Nina Amenta  
Alexandr Andoni  
Patrizio Angelini  
Hyojeong Ann  
Elena Arseneva  
Sunil Arya  
Dominique Attali  
Sang Won Bae  
Håvard Bakke Bjerkevik  
Nikhil Balaji  
Martin Balko  
Igor Balla  
Aritra Banik  
Imre Bárány  
Jeremy Barbay  
Agnese Barbensi  
Abdul Basit  
Aniket Basu Roy  
Matias Bender  
Paul Bendich  
Mark de Berg  
Thijs Beurskens  
Sujoy Bhore  
Michael Bilevich  
Davide Bilò  
Jarosław Błasiok  
Thomas Bläsius  
Jannis Blauth  
Bea Bleile  
Johannes Bloemer  
Omer Bobrowski  
Greg Bodwin  
Prosenjit Bose  
Magnus Botnan  
Robyn Brooks  
Anna Brötzner  
Kevin Buchin  
Matija Bucic  
Michael Burr  
Sergio Cabello  
Jean Cardinal  
Mathieu Carrière  
Maria Rita Casali  
Lawrence Cayton  
Parinya Chalermsook  
Erin Chambers  
Timothy Chan  
Hsien-Chih Chang  
Bernard Chazelle  
Chandra Chekuri

40th International Symposium on Computational Geometry (SoCG 2024).

Editors: Wolfgang Mulzer and Jeff M. Phillips



LIPIC

Leibniz International Proceedings in Informatics

Schloss Dagstuhl – Leibniz-Zentrum für Informatik, Dagstuhl Publishing, Germany



**0:xviii Additional Reviewers**

Jingbang Chen	Jeff Erickson
Siu-Wing Cheng	Emerson Escolar
Otfried Cheong	Esther Ezra
Yi-Jen Chiang	Chenglin Fan
Aruni Choudhary	Sándor Fekete
Chaeyoon Chung	Stefan Felsner
Jaehoon Chung	Alex Fernandes
Ken Clarkson	Arnold Filtser
David Cohen-Steiner	Nick Fischer
Éric Colin de Verdière	Henry Förster
Marco Contesotto	Emily Fox
Ryan Cotsakis	Bin Fu
Guilherme D. da Fonseca	Radoslav Fulek
Justin Dallant	Waldo Gálvez
Gábor Damásdi	Junhao Gan
Rathish Das	Jie Gao
Jean-Lou De Carufel	Bernd Gärtner
Vincent Despré	Tzvika Geft
Luc Devroye	Panos Giannopoulos
Walter Didimo	Barbara Giunti
Hu Ding	Marc Glisse
Michael Gene Dobbins	Xavier Goaoc
Lukas Drexler	Petr A. Golovach
Anne Driemel	Timothy Gomez
Fabien Dufoulon	Rocio Gonzalez-Diaz
Vida Dujmovic	Mayank Goswami
Adrian Dumitrescu	Ryan Grady
Kunal Dutta	Christoph Grunau
Alon Efrat	Joachim Gudmundsson
Alex Elchesen	Siddharth Gupta
Henrique Ennes	Michel Habib
Taekang Eom	Dan Halperin
David Eppstein	Thekla Hamm

Ramon van Handel	Haim Kaplan
Kristoffer Arnsfelt Hansen	Julia Katheder
Farouk Harb	Eleni Katsanou
Alexander He	Matthew J. Katz
Teresa Heiss	Michael Kaufmann
Annika Hennes	Michael Kerber
Didier Henrion	Balázs Keszegh
Gregory Henselman-Petrusek	Arindam Khan
John Hershberger	Liana Khazaliya
Yasuaki Hiraoka	Geunho Kim
Jan Hladký	Hwi Kim
Winfried Hochstättler	Minki Kim
Ivor van der Hoog	Woojin Kim
Max Hopkins	Philipp Kindermann
Samuel Hornus	Evangelos Kipouridis
Thijs van der Horst	Sándor Kisfaludi-Bak
Tao Hou	Linda Kleist
Xiao Hu	Boris Klemz
Zengfeng Huang	Bettina Klinz
Stefan Huber	Fabian Klute
Kristóf Huszár	Dusan Knop
John Iacono	Tomasz Kociumaka
Tanmay Inamdar	Lili Ködmön
R. Inkulu	Tuukka Korhonen
Oliver Janzer	Matias Korman
Bruno Jartoux	Peter Kramer
Attila Jung	Bala Krishnamoorthy
Mook Kwon Jung	Myroslav Kryven
Praneeth Kacham	Nirman Kumar
Matthew Kahle	Pankaj Kumar
Gil Kalai	Jan Kynčl
Byeonguk Kang	Jeffrey Lagarias
Seokyun Kang	Claudia Landi

Hung Le	Cameron Musco
Vadim Lebovici	Christopher Musco
Jaegun Lee	Nabil Mustafa
Seungjun Lee	Torsten Mütze
Erik Jan van Leeuwen	Vijay Natarajan
Clément Legrand-Duchesne	Amir Nayyeri
Michael Lesnick	Jesper Nederlof
Joshua Levine	Ofer Neiman
Jingyi Li	Yakov Nekrich
Bernard Lidický	Andrew Newman
André Lieutier	Aleksandar Nikolov
William Lochet	Bengt Nilsson
David Loiseaux	Gabriel Nivasch
Andres López Martínez	André Nusser
Martin Lotz	Joseph O'Rourke
Alexandre Louvet	Johannes Obenaus
Anna Lubiw	Eunjin Oh
Angelos Mantzaflaris	Tim Ophelders
Yannic Maus	Jakub Opršal
Daniel McGinnis	Giacomo Ortali
Brendan McKay	Joachim Orthaber
Manor Mendel	Igor Pak
Arturo Merino	Irene Parada
Victor Milenkovic	Pavel Paták
Lazar Milenković	Amit Patel
Ezra Miller	Florian Pausinger
Majid Mirzanezhad	Yuval Peled
Joseph Mitchell	Richard Peng
Debajyoti Mondal	Sarah Percival
Fabrizio Montecchiani	Pablo Pérez-Lantero
Shlomo Moran	François Petit
Julie Mordacq	Julian Pfeifle
Liz Munch	Maximilian Pfister

Vincent Pilaud	Marcus Schaefer
Michał Pilipczuk	Manfred Scheucher
Lukas Plätz	Maximilian Schmahl
Valentin Polishchuk	Christiane Schmidt
Aleksandr Popov	Patrick Schnider
Marc Pouget	Jens Kristian Refsgaard Schou
Lionel Pournin	Hannah Schreiber
Siddharth Pritam	Felix Schröder
Ioannis Psarros	Chris Schwiegelshohn
Saladi Rahul	Luis Scoccola
Rajiv Raman	Eric Sedgwick
S. Srinivasa Rao	Donald Sheehy
Abhishek Rathod	Anastasios Sidiropoulos
Meghana M. Reddy	Francesco Silvestri
Carolin Rehs	Kirill Simonov
André van Renssen	Primož Skraba
Bastian Rieck	Michiel Smid
Christian Rieck	Shakhar Smorodinsky
Yo'av Rieck	Jack Snoeyink
Liam Roditty	Shay Solomon
Heiko Röglin	Matthias Söls
Alexander Rolle	Jongbaek Song
Jonathan Rollin	Minju Song
Günter Rote	Jan Soukup
Bodhayan Roy	Michela Spagnuolo
Sasanka Roy	Bettina Speckmann
Benjamin Ruppik	Jonathan Spreer
Florian Russold	Frank Staals
Paweł Rzażewski	Fabian Stehn
Arsenii Sagdeev	Raphael Steiner
Eric Samperton	Peter Stumpf
Maria Saumell	Martin Suderland
Saket Saurabh	Shuhao Tan

**0:xxii Additional Reviewers**

Cuong Than

Raphaël Tinarrage

Istvan Tomon

Ngoc Tran

Konstantinos Tsakalidis

Torsten Ueckerdt

Ali Vakilian

Pavel Valtr

Kasturi Varadarajan

Narmada Varadarajan

Kevin Verbeek

Ziga Virk

Hubert Wagner

Bartos Walczak

Zhengchao Wan

Haitao Wang

Qingsong Wang

Karol Wegrzycki

Alexandra Wesolek

Sebastian Wild

Mathijs Wintraecken

Sampson Wong

Geert van Wordragen

Kaiyu Wu

Cheng Xin

Yinzhan Xu

Jie Xue

Pavlo Yatsyna

Ke YI

Yelena Yuditsky

Joshua Zahl

Nicolo Zava

Meirav Zehavi

Ji Zeng

Shira Zerbib

Da Wei Zheng

Samson Zhou

Binhai Zhu

Lori Ziegelmeier

Kristóf Zólomy

Pawel Zylinski