# Engineering Time-Expanded Graphs for Faster Timetable Information ${ }^{\star}$ 

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#### Abstract

We present an extension of the well-known time-expanded approach for timetable information. By remodeling unimportant stations, we are able to obtain faster query times with less space consumption than the original model. Moreover, we show that our extensions harmonize well with speed-up techniques whose adaption to timetable networks is more challenging than one might expect.


## 1 Introduction

During the last years, many speed-up techniques for computing a shortest path between a given source $s$ and target $t$ have been developed. The main motivation is that computing shortest paths in graphs is used in many real-world applications like route planning in road networks or timetable information for railways. Although DIJKSTRA's algorithm [5] can solve this problem, it is far too slow to be used on huge datasets. Thus, several speed-up techniques have been developed (see [4] for an overview) yielding faster query times for typical instances. However, recent research focused on developing speed-up techniques for road networks, while only few work has been done on adapting techniques to graphs deriving from timetable information systems. In general, two approaches exist for modeling timetable information: The time-dependent and timeexpanded approach. While the former yields smaller inputs (and hence, smaller query times), the latter allows a more flexible modeling of additional constraints. It turns out that adaption of speed-up techniques to each of these models is more challenging than one might expect.

In this work, we use a different approach for obtaining faster query times. Instead of applying a routing algorithm, e.g., plain DIJKSTRA, on the original model, we improve the time-expanded model itself in such a way that a routing algorithm does not exploit parts of the graph not necessary for solving the earliest arrival problem (EAP). Interestingly, it turns out that those optimizations are included in the time-dependent approach implicitely. By introducing those techniques to the time-expanded approach, query times for the time-expanded approach are comparable to the time-dependent approach.

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### 1.1 Related Work

The simple, i.e., without realistic transfers, time-expanded model has been introduced in [21]. The model has been generalized in [18] in order to deal with realistic transfers. Since then, this realistic model has been used for many experimental studies, e.g., [14, 19, 2]; most of them focusing on faster speed-up techniques or multi-criteria optimization for timetable information. However, [21] enriched the simple time-expanded graph by shortcuts and [19] introduced minor changes to the time-expanded model itself by removing unnecessary nodes with outgoing degree 1 .

### 1.2 Our Contributions

This paper is organized as follows. Section 2 includes formal definitions and a review of the time-expanded model for timetable information. Our main contribution is Section 3. We show how the main ingredient for high-performance speed-up techniques in road networks, i.e., contraction, can be adapted to time-expanded graphs. Unfortunately, it turned out that this contraction yields a tremendous growth in number of edges (unlike in road networks). However, by changing the modeling of unimportant stations, a DIJKSTRA does not exploit unnecessary parts of the network. The key observation is the following. Assume $T$ is a station with only one line stopping. A passenger traveling via $T$ only leaves the train if $T$ is her target station, otherwise it never pays off to leave the train. Moreover, we are able to generalize this approach to stations with more lines stopping at that station. In Section 4 we introduce a new speed-up technique tailored to time-expanded graphs based on blocking certain connections. Furthermore, we show how existing techniques have to be adapted to timetable graphs. It turns out that certain pitfalls exist that one might not expect. However, those adapted techniques harmonize well with our new approaches, which we confirm by an experimental evaluation in Section 5 . We conclude our work in Section 6 with a summary and future work.

## 2 Preliminaries

Throughout the whole work, we restrict ourselves to the earliest arrival problem (EAP), i.e., find a connection in a timetable network with lowest travel time. In the following we often call this single-criteria search in contrast to multi-criteria search that also minimizes number of transfers and further criteria [14, 19].

Moreover, we restrict ourselves to simple, directed graphs $G=(V, E$, length) with positive length function length : $E \rightarrow \mathbb{R}^{+}$. The reverse graph $\bar{G}=(V, \bar{E})$ is the graph obtained from $G$ by substituting each $(u, v) \in E$ by $(v, u)$. A partition of $V$ is a family $\mathscr{P}=\left\{P_{0}, P_{1}, \ldots, P_{k}\right\}$ of sets $P_{i} \subseteq V$ such that each node $v \in V$ is contained in exactly one set $P_{i}$. An element of a partition is called a cell. The boundary nodes $B_{P}$ of a cell $P$ are all nodes $u \in P$ for which at least one node $v \in V \backslash P$ exists such that $(v, u) \in E$ or $(u, v) \in E$.

The Condensed Model is the easiest approach for modeling timetable information. Here, a node is introduced for each station and an edge is inserted iff a direct connection
between two stations exists. The edge weight is set to be the minimum travel time over all possible connections between these two stations. Unfortunately, several drawbacks exist. First of all, this model does not incorporate the actual departure time from a given station. Even worse, travel times highly depend on the time of the day and the time needed for changing trains is also not covered by this approach. As a result, the calculated travel time between two arbitrary stations in such a graph is only a lower bound of the real travel time. However, in Section 4 we show that the condensed model is helpful for certain speed-up techniques.

The (Realistic) Time-Expanded Model. Throughout this work, we use the realistic time-expanded model allowing realistic queries. Therefore, three types of nodes are used to represent certain events in the timetable. Departure and arrival nodes are used to model elementary connections in the timetable. Thus, for each elementary connection $c \in \mathscr{C}$ one arrival and departure node is created and an edge is inserted between them. To model transfers, transfer nodes are introduced. For each departure event one transfer node is created which connects to the respective departure node having weight 0 . To ensure a minimum transfer time $\operatorname{TranSFER}(S)$ at a specific station $S$, an edge from each arrival node $u$ is inserted to the smallest (considering time) transfer node $v$ where $\Delta(\operatorname{TimE}(u), \operatorname{TimE}(v)) \geq \operatorname{TRANSFER}(S)$. Here $\Delta(\cdot, \cdot)$ denotes the time difference between two points in time and TIME : $V \rightarrow \mathscr{T}$ maps each node to its timestamp with respect to the timetable. Due to the periodic nature of our timetables $\Delta$ is defined by

$$
\Delta\left(t_{1}, t_{2}\right):= \begin{cases}t_{2}-t_{1} & \text { if } t_{2} \geq t_{1} \\ t_{2}+1440-t_{1} & \text { otherwise }\end{cases}
$$

To ensure the possibility to stay in the same train when passing through a station, an additional edge is created which connects the arrival node with the appropriate departure node belonging to this same train. Further to allow transfers to an arbitrary train, transfer nodes are ordered non-decreasing. Two adjacent nodes (w.r.t. the order) are connected by an edge from the smaller to the bigger node. Furthermore, to allow transfers over midnight, an overnight-edge from the biggest to the smallest node is created. For further details, see [19].

For each edge $e=(u, v)$ in the expanded graph the weight $w(e)$ is defined as the time difference $\Delta(\operatorname{TIME}(u), \operatorname{TIME}(v))$ of the nodes the edge connects. Hence, we call the graph consistent in time, meaning for each path from $u$ to $v$ in the graph, the sum of the edge weights along the paths is equal to the time difference $\Delta(\operatorname{TIME}(u), \operatorname{TIME}(v))$.

For future considerations the following notation will be helpful. Let $\prec \subseteq V \times V$ be a relation which compares two events in time. Since in the expanded model nodes correspond to events with a certain timestamp, our relation is defined on the set of nodes of the graph. We say for two nodes $u, v \in V$ that $u \prec v$ if the event of $u$ is happening before the event of $v$. Please note that it cannot be determined for $u$ and $v$ if $u \prec v$ just by comparing $\operatorname{TimE}(u)$ and $\operatorname{TiME}(v)$ due to the periodic nature of the timetable and the fact that times are always expressed in minutes after midnight. If for example $\operatorname{TIME}(u)=$ 400 and $\operatorname{Time}(v)=600$ there are two possibilities. Either $u \prec v$ with $\Delta(u, v)=200$ or $v \prec u$ with $\Delta(v, u)=1640$. As a consequence, the $\Delta$ function applied to a tuple $(u, v)$ is only valid if $u \prec v$.

## 3 Engineering the Time-Expanded Model

In this section, we present approaches how to enhance the classical time-expanded model. Our first attempt applies a technique deriving from road networks, i.e., contraction, to railway graphs. However, it turns out that this approach yields a too high number of edges. Hence, we also introduce the Route-Model which changes the modeling of "unimportant" stations.

### 3.1 Basic Contraction

All speed-up techniques developed during the last years have one thing in common. During preprocessing they apply a contraction routine, i.e., a process that removes unimportant nodes from the graph and adds shortcuts to the graph to keep the distances between the remaining nodes correct. Interestingly, the fastest hierarchical technique for routing in road networks, Contraction Hierarchies [6], relies only on such a routine. The key observation is that in road networks, the average degree of remaining nodes does not explode.

At a glance, one could be optimistic that contraction also works well in railway networks. Like in road networks, some nodes in time-expanded graphs are more important than others. However, contraction does not exploit the special structure of timeexpanded timetable graphs. For example, departure nodes have an outgoing degree of 1. Thus, we can safely remove such nodes and add a shortcut between the corresponding transfer and arrival node. More precisely, we propose a new contraction routine consisting of three steps. In the following we explain each step separately.

Omitting Departure Nodes The first step of our contraction routing bypasses all departure nodes. In [19], the authors state that departure nodes can be omitted in time-expanded graphs which can be interpreted as bypassing those nodes.
Omitting Arrival Nodes In a second step, we bypass all arrival nodes within the network. As a consequence, the degree of transfer nodes highly increases. By these two steps we reduce the number of nodes by approximately a factor of 3 . However, the graph still contains all original transfer nodes of which some are more important than others.
Bypass Transfer Nodes The final step of our contraction bypasses nodes according to their degree. We bypass nodes with low degree first yielding changes in the degree of its neighbors. Our contraction ends if all transfer nodes have a total degree at least of $\delta$, which is a tuning parameter. We suggest to use a min-heap to determine the next node to be bypassed. The key of a node $x$ shall be $\operatorname{deg}_{\text {in }}(x)+\operatorname{deg}_{\text {out }}(x)$.

Note that we need not apply all three steps. While the first step reduces both number of nodes and edges, the following two steps yield higher edge counts. In the following, we call a time-expanded model with shortcut departure nodes, the phase 1 model. The phase 2 model has neither arrival nor departure nodes. If we also remove (some) transfer nodes, we call the resulting graph a phase 3 graph. For an experimental evaluation of this contraction routine, see Section 5.

### 3.2 Route-Model

In our experimental studies, it turned out that our contraction routine from the last section suffers from a dramatic growth in number of edges. Already our phase 2 model has up to 3.6 times more edges than the original graph (cf. Section 5). Hence, we here introduce a different approach, called the route model. In contrast to contraction, we exploit certain semantic properties of the time expanded graph regarding transferring which eventually leads to a reduction of the number of shortest paths. The classic timeexpanded model allows transfers at a station from each arriving train to all subsequent departing trains. However, when planning an itinerary by hand, we would probably do the following intuitive pruning: During the way from the source to the target station assume we find a route which leads to some station $S$ on the way, arriving there at time $t_{S}$. Then, we would not need to examine paths toward station $S$ with an arrival time $t_{S}^{\prime}>t_{S}$, since computing these paths is redundant as we already arrived at $S$ earlier, and we could achieve the same result by taking the earlier computed path arriving at $S$ at $t_{S}$ and then waiting at $S$ until $t_{S}^{\prime}$. This observation is the basic idea behind the route model.

Remodeling of Stations. The modifications to the (original realistic) time-expanded graph are done locally and independently for each station $S$, and involve the following three steps:

1. Remove all outgoing edges from all arrival nodes. This includes edges to transfer nodes as well as edges to the departure node of the same train.
2. Insert a minimal number of new transfer-edges directly from the arrival nodes to departure nodes. This allows us to model transfers more specific without losing any optimal shortest paths in comparison to the original time expanded model.
3. Keep the transfer nodes and their interconnecting edges as well as departure-edges from transfer to departure nodes. Although, there are no more edges in the graph to get from an arrival node to a transfer node, the transfer nodes are still used as source nodes for the actual DIJKSTRA query.

The only non-trivial modification is the second one, where for each arrival node we need to find a minimal set of departure nodes which shall become reachable from the particular arrival node. For that reason let $S$ be the currently considered station and $\mathscr{N}_{S}$ all neighbors of $S$. A station $T \in \mathscr{N}_{S}$ is called a neighbor of $S$ if at least one elementary connection from $S$ to $T$ exists. Thus, we can speak of routes between $S$ and each neighbor from $\mathscr{N}_{S}$. We now use the following notation. $u$ denotes an arbitrary but fixed arrival node of $S$ from which outgoing edges are inserted. $v$ denotes the departure node toward which the edges $(u, v)$ are inserted. Furthermore, $w$ denotes the arrival node corresponding to the elementary connection to which the departure node $v$ belongs. The basic idea is to insert (at least) one edge per route toward a departure node belonging to the the particular route. So, let us consider some fixed station $T \in \mathscr{N}_{S}$ with $T \neq R$ where $R$ is the station where we just came from through $u$. Of all departure nodes $v$ belonging to an elementary connection $(v, w)$ from $S$ to $T$ we insert an edge $(u, v)$ in $S$ according to the following criteria.

1. The node $w$ is the smallest (regarding time) possible (meaning it is not in violation with the second criterion) arrival node at $T$ that is after $u$, i.e. $w \succ u$.
2. The node $v$ respects the transfer time criterion at $S$. For that reason it has to hold that $v \succ u+\operatorname{TRANSFER}(S)$ if $u$ and $v$ belong to different trains, or $v \succ u$ if they share the same train.

Obviously, by this strategy we select the edge $(u, v)$ according to the earliest possible arrival event at the target station $T$. This yields a transfer to a train which arrives at $T$ by the earliest possible time. Note that if we instead would have chosen $v$ according to the earliest possible departure node at $S$, we could have missed a different train that departs at $S$ later, but arrives at $T$ earlier. Such a scenario is called overtaking of trains. Also note, that if the train belonging to $u$ utilizes the route toward station $T$, it does not necessarily have to be the case, that the inserted edge $(u, v)$ corresponds to the departure event of that specific train. It simply corresponds to the train arriving at $T$ first, which may well be a different train.

Transfer Times at Neighboring Stations. While we did respect the transfer time criterion of $S$, we also have to respect the transfer time criterion at $T$. Figure 1 shows why this is important.

(a)

(b)

Fig. 1: Two problems concerning the transfer time criterion at station $T$.

On the left side the train $Z_{2}$ arriving at $T$ just slightly after $Z_{1}$ is the optimal path, but it can not be transferred to, because at $S$ we only chose $Z_{1}$ and at $T$ the transfer time is too big to reach it from $Z_{1}$. On the right picture the scenario is even worse. While the train $Z_{1}$ is the earliest train regarding the arrival time at $T$, the optimal route again contains $Z_{2}$ which departs at $S$ earlier than $Z_{2}$, but it is not reachable because it arrives at $T$ slightly after $Z_{1}$. Again the transfer time at $T$ is too big to enter $Z_{2}$ at $T$. In both cases we have to ensure that $Z_{2}$ can be entered somewhere. Since our modifications should remain local in the sense that modifications at $S$ should not involve modifications at some other stations, we ensure that $Z_{2}$ can be reached at $S$.

By adding some more edges to the graph, we are able to allow those connections as well. Let $w_{\text {earl }}$ denote the earliest arrival node at $T$ as computed before. Then, we insert edges $(u, v)$ (belonging to connections $(v, w))$ satisfying the following properties.

1. Consider all trains arriving after $w_{\text {earl }}$ but no later than the transfer time at $T$, mean$\operatorname{ing} w \succ w_{\text {earl }}$ and $w \prec w_{\text {earl }}+\operatorname{TRANSFER}(T)$.
2. Still respect the transfer time criterion at $S$, i.e. $v \succ u+\operatorname{TRANSFER}(S)$ if $u$ and $v$ belong to different trains and $v \succ u$ otherwise.

This routine ensures that (a) it is possible to arrive at $T$ as early as possible and (b) all trains that go through $T$ within the margin between the earliest arrival time and the transfer time at $T$ can be reached by entering them at $S$.

Uncommon Routes. Despite these modifications, we additionally have to deal with another phenomenom in railway networks. In very few cases, it might pay off to use an itinerary with a sequence of stations $R \rightarrow S \rightarrow T \rightarrow S \rightarrow R^{\prime}$ instead of $R \rightarrow T \rightarrow R^{\prime}$. This odd situation may arise if $T$ and $S$ are close to each other, a train runs from $R$ to $T$, another from $T$ to $R^{\prime}$, and $\operatorname{TranSFER}(S)<\operatorname{TranSFER}(T)$ holds. Figure 2 gives an example.


Fig. 2: Situation where it is necessary to go forth and back along the same route in order to transfer to train $Z_{2}$.

Our Route-Model does not allow such connections. However, we may overcome this problem by introducing edges at arrival nodes $u$ of $S$ toward departure nodes leading back to $R$ if and only if the following inequation holds:

$$
\kappa_{R, S}+\kappa_{S, R}+\operatorname{TRANSFER}(S)<\operatorname{TRANSFER}(R)
$$

Here $\kappa_{R, S}$ denotes the best lower bound regarding travel time from $R$ to $S$. By this we ensure that no shortest paths get lost while in most cases we still get the advantage of prohibiting cycles along the same route. Please note, that we can not rule out cycles such as $\cdots \rightarrow R \rightarrow S \rightarrow T \rightarrow R \rightarrow \cdots$, however cycles of this type occur less often in general timetable networks.

Leaving Big Stations Untouched. It turns out that remodeling of stations with many neighbors, e.g., major train hubs, lead to a disproportionately high increase in additional edges, since for each neighbor (route) at least one edge must be inserted for each arriving train. In the original time expanded model, however, at most two edges existed for each arrival node (arrival-transfer and arrival-departure). Since our modifications
are only local we can choose for each station individually whether we want to convert it to the Route-Model or not. For that reason we introduce a tuning parameter $\gamma$ indicating that stations with more neighbors than $\gamma$ should be left untouched. Hence, changing $\gamma$ yields a trade-off between a speed-up regarding the number of touched nodes against an increasing size of the edge set of the graph.

A problem that arises when mixing Route-Model stations with classic stations is that the main advantage of the Route-Model-subsequent connections on the same route are not visited during the DIJKSTRA search—may fade. Analyzing the example in Figure 3, we observe a big station which has not been converted followed by a route containing a few small stations. While at the small stations no connections exist between connections of the same route, they are nevertheless visited, because they are all accessible through the big station. Hence, we developed Node-Blocking which adopts the idea behind the Route-Model as a speed-up technique, and blocks redundant connections of the same route, so they are not visited. This technique is explained in Section 4.

Theorem 1. Applying Diskstra on the Route-Model yields correct solutions to the earliest arrival problem.

The proof of Theorem 1 can be found in the full paper.

## 4 Speedup Techniques

In principle, we could use DiJkstra's algorithm for solving EAP. However, plain DIJKSTRA visits unnecessary parts of the graph, even if we use our Route-Model. Hence, we introduce two approaches for obtaining faster query times. We adapt existing techniques-developed for road networks-to timetable graphs and introduce a new speed-up technique following the ideas from our Route-Model.

$$
\text { Big Station } \quad \text { Small Station } \quad \text { Small Station }
$$



Fig. 3: When a big station which is not converted is visited during a DIJKStra query, all subsequent connections are visited as well, while only the red path should be relevant. Unimportant nodes are omitted in the figure.

### 4.1 Tailored Speed-Up Techniques

Node-Blocking is a speed-up technique tailored to time-expanded networks. It basically incorporates the ideas behind the Route-Model as described in Section 3.2: if we can reach a station $S$ at some time $t_{S}$ we try to prune paths reaching $S$ at a later time $t_{S}^{\prime}>t_{S}$. Recall that the Route-Model prunes the search by removing certain edges from the graph. Node-Blocking, on the contrary, achieves a similar result by dynamically blocking departure nodes during the DiJKSTRA query. The idea is as follows. If we visit a departure node $v$ belonging to an elementary connection targeting some station $T$, we can prune all future departure nodes $b$ targeting $T$.

Preprocessing. Formally, each departure node $v$ of an elementary connection between two stations $S$ and $T$ induces a set $B_{v}$ of blocked nodes. A node $b$ is contained in $B_{v}$ if and only if the following conditions hold.

1. $b$ is a departure node at $S$ belonging to an elementary connection targeting the same station $T$ as $v$.
2. $b \succ v$ holds.
3. If $w$ and $c$ are the arrival nodes at $T$ of the connections associated with $v$ and $b$, respectively, then $w+\operatorname{TRANSFER}(T) \prec c$ must hold, i.e., we respect the transfer time criterion at $T$.

Although the "blocked state" of each node is dynamic in the sense that it depends on the shortest path query, and therefore must be computed during the query, the set $B_{v}$ of inducing blocked nodes can be precomputed for each node $v$ by iterating through all departure nodes of the station and checking whether the above criteria apply to them.

Note that in contrast to the Route-Model, we do not have to deal with the transfer time criterion at $S$, since we only block nodes, and hence never allow a path to be taken which was forbidden by the transfer time criterion at $S$. In worst case, we block departure nodes which cannot be reached anyway due to the transfer time criterion of $S$. Moreover, all special cases are covered by our third condition.

Query. The modifications to standard DiJKstra algorithm are simple. We introduce an additional flag blocked $(v)$ to all nodes of the graph, which is initialized to false. Then, whenever we try to insert a node $v$ into the queue, we mark all nodes $B_{v}$ as blocked. If $v$ is marked as blocked, we prune the search.

Combination with Route Model. Although our Route-Model and Node-Blocking follow the same ideas, the advantage of the Route-Model is the lower computation-overhead during the query. However, as discussed in Section 3.2, it does not pay off to remodel major hubs. Hence, Node-Blocking harmonizes well with the Route-Model as we use Node-Blocking for pruning paths at such hubs.

Combination with Phase $1+$ Models. Since from the Phase 1 model onwards departure nodes are removed, Node-Blocking has to be altered slightly to conform with these models. Instead of departure nodes blocking future departure nodes, we simply let the corresponding arrival nodes (belonging to the respective departure nodes) block each other. In this case, the arrival nodes assume the role of the previous departure nodes regarding blocking, which allows us to continue using the same query algorithm.

## Theorem 2. Applying Node-Blocking to DiJKSTRA's algorithm yields correct solutions to the earliest arrival problem.

The proof of Theorem 2 can be found in the full paper.

### 4.2 Adapting Speed-Up Techniques

Although the adaption of many techniques may be promising, we choose basic goaldirected techniques for adaption. It turned out that adaption of more sophisticated techniques, e.g., Highway Hierarchies [20], Contration Hierarchies [6], REAL [8], SHARC [1], is much more challenging than expected. The main reason are either the need of a bidirectional query algorithm or the bad performance of the contraction routine.

Arc-Flags. The classic Arc-Flag approach, introduced in [13, 12], first computes a partition $\mathscr{P}$ of the graph and then attaches a label to each edge $e$. A label contains, for each cell $P_{i} \in \mathscr{P}$, a flag $A F_{P_{i}}(e)$ which is true if a shortest path to at least one node in $P_{i}$ starts with $e$. A modified Diskstra-from now on called Arc-Flags Diskstra-then only considers those edges for which the flag of the target node's cell is true. The big advantage of this approach is its easy query algorithm. However, preprocessing is very extensive. The original approach grows a full shortest path tree from each boundary node yielding preprocessing times of several weeks for instances like the Western European road network. Recently, a new centralized approach has been introduced [11]. However, it turns out that this centralized cannot be used in time-expanded transportation networks due to memory consumption. Hence, we use the original approach of growing full shortest path trees from each node.

Adaption. The query algorithm can be adapted to time expanded railway graphs very easily. We only have to consider that the exact target node is unknown (just the target station is known). For that reason we simply abort the DiJKstra algorithm as soon as a node belonging to the target station is settled. The preprocessing of Arc-Flags, however, needs some extra attention. Since we do not know the exact target node in advance, we have to ensure that all nodes belonging to the same station also get the same cell-id of the partition assigned. For that reason, we simply compute the partition on the condensed graph and map it to the expanded graph by assigning for each node $v \in V$ the cell-id due to $\operatorname{cell}(v):=\operatorname{cell}(\operatorname{station}(v))$.

Computing the backwards-shortest path trees from each boundary node of each cell can then be done as described in [13]. However, this approach yields a problem specific on time expanded graphs. Since the length of any path in the graph always corresponds to the time needed to travel between the beginning and ending event (node) of that particular path, any two different paths between the same nodes always have the same length. Therefore, the number of shortest paths (in fact, there are only shortest paths in time expanded graphs) is tremendous. Unfortunately, if we set flags to true for every path, we do not observe any speed-up (cf. Section 5). In order to achieve a speed-up we have to prefer some paths over others. We examine the following four reasonable strategies for prefering paths:

Hop Minimization. For two paths of equal length, choose the one that has less hops (nodes) on it. This approach is often used in road networks [1].
Transfer Minimization. Choose the path that has less transfers between trains. While this is a good strategy for querying, it sets too many arc-flags to true, since for different boundary nodes too many different paths lead a transfer-minimal connection.
Distance Minimization. Choose the path that is shorter (geographically).
Direct Geographical Distance. Choose the path whose direct geographical distance is closer to the source node of the shortest path tree, formally for some node $v$ that is reached from $u$ we choose the new predecessor according to

$$
\operatorname{pre}(v)_{\text {new }}:=\underset{w \in\{u, \operatorname{pre}(v)\}}{\operatorname{argmin}}\left\{\sqrt{\left(\operatorname{coord}_{x}(w)-\operatorname{coord}_{x}(s)\right)^{2}+\left(\operatorname{coord}_{y}(w)-\operatorname{coord}_{y}(s)\right)^{2}}\right\},
$$

where $s$ is the source node of the shortest path tree. This optimization is very aggressive, as it leads to the same result for different boundary nodes of the same cell as often as possible.

Section 5 shows the huge difference in the query performance when the arc-flags are computed with different strategies. Note that we can optimize query times by setting as many flags as possible to false. However, we also loose the ability to choose the "best" path during the query (e.g. due to a minimal number of transfers, costs, etc.). This yields a trade-off between query time and the quality of the computed itineraries.

Arc-Flags and Node-Blocking. Unfortunately, Node-Blocking does not harmonize with Arc-Flags. This is due to the fact of Node-Blocking being a very aggressive technique, leaving only very few connection arcs per station and route accessible. The optimization criterion hereby, namely arriving as early as possible at the next station does not necessarily match with our path selection during Arc-Flags preprocessing. As a result, both techniques prune different shortest paths. A possible solution would be to adapt the path selection for Arc-Flags according to Node-Blocking. However, this turns out to be complicated as we have to grow shortest path trees on the reverse graph. Hence, this path selection strategy is not implemented yet.

ALT. Goal directed search, also called $A^{*}$ [10], pushes the search towards a target by adding a potential to the priority of each node. The ALT algorithm, introduced in [7], uses a small number of nodes-so called landmarks-and the triangle inequality to compute such feasible potentials. Given a set $L \subseteq V$ of landmarks and distances $d(\ell, v), d(v, \ell)$ for all nodes $v \in V$ and landmarks $\ell \in L$, the following triangle inequations hold: $d(u, v)+d(v, \ell) \geq d(u, \ell)$ and $d(\ell, u)+d(u, v) \geq d(\ell, v)$. Therefore, $\pi(u, t):=\max _{\ell \in L} \max \{d(u, \ell)-d(t, \ell), d(\ell, t)-d(\ell, u)\}$ provides a lower bound for the distance $d(u, t)$ and, thus, can be used as a potential for $u$.

Adaption. The query algorithm is, again, straight forward to adapt to time-expanded railway graphs. Since the only difference to the standard DIJKSTRA algorithm is the key which is inserted into the priority queue, we can still simply abort the search as soon as a node of the target station gets settled. However, we cannot compute the landmarks
on the expanded graph directly since then we would have to know the target node $t$ in advance. Hence, we compute the landmarks on the much smaller condensed graph which still yields feasible potentials because the edge weights in the condensed graph are defined as the lower bounds regarding travel time. The potential function $\pi$ during the query is then computed as follows:

$$
\pi(v)=\max _{\ell \in L} \max \{\operatorname{dist}(\operatorname{STATION}(v), \ell)-\operatorname{dist}(T, \ell), \operatorname{dist}(\ell, T)-\operatorname{dist}(\ell, \operatorname{STATION}(v))\}
$$

where $T$ is the target station of the query. We can think of this as using a "lower bound of a lower bound" of the shortest path.

Former studies revealed that the selection of landmark nodes is crucial to the performance of ALT. The quality of the lower bounds highly depends on the quality of the selected landmarks. Thus, several selection strategies exist. To this point, no technique is known how to pick landmarks yielding the smallest search space for random queries. Thus, several heuristics exist. The best are avoid and maxCover. The first tries to identify regions that are not well covered by landmarks while the latter is basically the avoid routine followed by a local optimization. For details, we refer to [9].

Due to the small size of the condensed networks, another strategy for obtaining potentials seems promising. For each query, we use the target station $T$ as landmark and compute the distances of all stations to $T$ on-the-fly. The advantage of this dynamic-landmark-selection is a tighter lower bound. However, we have to run a complete DIJKSTRA in the condensed graph for each query which can take more time than using worse lower bounds from landmarks during the query. Note that this approach for obtaining lower bounds for $\mathrm{A}^{*}$ was already proposed in [14].

Combining Arc-Flags and ALT. In [16], we observed that Arc-Flags (with the direct geographical distance strategy) and ALT optimize in two different ways. While Arc-Flags prunes paths that lead to the wrong direction geographically, ALT optimizes in time in the sense that fast trains are preferred over slow trains. Fast trains (having less stops in between) tend to get near the target station faster, yielding a lower key in the priority queue regarding the lower bound function. For that reason, it is suggestive to examine the combination of the two speed-up techniques. The implementation is straight-forward, since Arc-Flags does not interfere with ALT-Arc-Flags simply ignores edges that do not have their appropriate flag set, and ALT just alters the key in the priority queue.

## 5 Experiments

In this section, we present our experimental evaluation. Our implementation is written in C++ using solely the STL. As priority queue we use a binary heap. Our tests were executed on one core of an AMD Opteron 2218 running SUSE Linux 10.3. The machine is clocked at 2.6 GHz , has 16 GB of RAM and $2 \times 1 \mathrm{MB}$ of L2 cache. The program was compiled with GCC 4.2, using optimization level 4.

Inputs. We use two inputs for our evaluation. The railway network of Central Europe and a local bus network of greater Berlin. Both networks have been provided by HAFAS for scientific use; the former network consists of 30,517 stations and 1,775,552 elementary connections. The corresponding figures for the latter are 2,874 and 744,005, respectively. While the network of Europe provides a good average structure for a railway network mixed of long-distance trains supported by short-distance trains, the bus network of Berlin consists of a very homogeneous structure, since there are almost no "long-distance" buses. Because of this and the very dense operations of buses with their short travel times between stations, it has already been shown [16] that this network seems to be a very hard instance for timetable information queries.

It should be noted that, while our timetable data is realistic, the transfer times at the stations were not available to us. Hence, we generated them at random and chose between 5 and 10 minutes for the railway and between 3 and 5 minutes for the bus network.

Default Settings. In the following, we report preprocessing times and the overhead of the preprocessed data in terms of additional bytes per node. We evaluate query performance by running 1000 random $s-t$ queries with source and target station picked uniformly at random. We fix the departure time to 7:00 am. We report the average number of settled nodes during the query as well as the average query time. The speed-up refers to the query time and is computed in reference to the classic time expanded model without any speed-up technique applied.

### 5.1 Models

Parameters. We start our experimental evaluation with parameter tests for our RouteModel. Recall that in the Route-Model we may affect the conversion process by the selection of $\gamma$ which controls the maximum number of neighbors a station may have in order to become a Route-Model station. In the following we use values between 2 and 10 for $\gamma$. Table 1 reports for both our inputs: the resulting size (in terms of number of edges) and query performance. Note that we do not report number of nodes, as the remodeling routine does not add or remove any nodes. We also enabled Node-Blocking (see Section 4.1).

We observe that for both instances the Route-Model yields a speed-up. Increasing $\gamma$ up to 5 increases performance, while values $>5$ do not pay off. This is mostly due to the fact that for both graphs the majority of stations has less or equal than 5 neighbors ( $91 \%$ for the Europe and even $99 \%$ for the Berlin network).

Concerning Europe with $\gamma<5$, we observe that the resulting graph has less edges than originally. Recall in the original graph the number of outgoing edges per arrival node is at most 2 (one toward the nearest transfer node and one toward the departure node of the same train). Hence, a decrease in number of the edges can only result from merely one edge being inserted for many arrival nodes at stations of degree 2. Interestingly, this observation of decreasing edges does not hold for our bus network which is due to the high density of the network: Because the stations are very close to each other, it often holds that the travel time to go forth and back between some stations $S_{1}$ and $S_{2}$ is less than TRANSFER $\left(S_{1}\right)$, which results in back-edges being inserted for

Table 1: The effect of $\gamma$ on the performance of the Route-Model with Node-Blocking enabled.

| $\gamma$-value | europe |  |  | $b v b$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Size \#edges | QUERY |  | Size | Query |  |
|  |  | \#settled [ms] | -up | \#edges | \#settled [ms] | d-up |
| reference | 8,505,951 | 1,161,696 534.7 | 1.00 | 3,694,253 | 151,379 37.6 | 1.00 |
| 2 | 7,912,584 | 411,836 202.4 | 2.64 | 3,785,680 | 91,591 27.4 | 1.37 |
| 3 | 8,035,324 | 359,294 171.7 | 3.11 | 4,292,849 | 74,963 25.2 | 1.49 |
| 4 | 8,332,816 | 329,413 158.3 | 3.38 | 5,059,228 | 63,438 25.1 | 1.50 |
| 5 | 8,729,619 | 313,046 154.1 | 3.47 | 5,437,647 | 59,670 25.4 | 1.48 |
| 6 | 9,071,974 | 303,460 153.9 | 3.47 | 5,625,277 | 57,990 25.6 | 1.47 |
| 7 | 9,396,276 | 297,831 155.1 | 3.45 | 5,768,926 | 56,994 25.8 | 1.46 |
| 8 | 9,712,940 | 292,482 156.4 | 3.42 | 5,782,375 | 56,921 25.7 | 1.46 |
| 9 | 9,936,119 | 289,036 158.7 | 3.37 | 5,782,375 | 56,921 25.8 | 1.46 |
| 10 | 10,195,050 | 285,103 159.3 | 3.36 | 5,782,375 | 56,921 25.8 | 1.46 |

arrival nodes at $S_{2}$ (coming from $S_{1}$ ). Second, the operation frequency of the buses is very high, such that it may occur that edges toward more than the first bus of the route are inserted, when they arrive at the next station within the margin of its transfer time.

Summarizing, a value of $\gamma=5$ yields the best results for railway input. The corresponding figure for the bus networks is 4 .

Comparison to the Classic Time-Expanded Model. Next, we compare different contraction steps (Section 3) and our route model with the classic time expanded model. Table 2 shows the differences in graph size and query performance. While the overall graph size decreases when switching from the classic expanded to the phase 1 model, the number of edges significantely increases if applying our phase 2 model. Although the number of nodes decreases about $50 \%$, this increase in number of edges leads to an worse query performance, since more edges are relaxed during the query. We hence conclude that the phase 2 model-and therefore the phase 3 model as well-is not the preferred choice for fast timetable queries.

Regarding the Route-Model, the increase in graph size is still reasonable while the query time decreases. However, we see, that the query performance benefits from NodeBlocking as the speed-up more than doubles in the Europe network with Node-Blocking enabled. The reason for the weak performance without Node-Blocking is that paths through the graph, that should be pruned by the Route-Model approach, are still relaxed when they are not blocked in non-converted big traffic hubs. In the bus network the general performance gain is not as big as with the railway network. Even NodeBlocking does not have such a great impact, which is mostly due to the dense structure of this network.

Because the Route-Model can be combined well with the phase 1 model (departure nodes are simply removed after the conversion to the Route-Model), this gives us a gain in graph size while still keeping the advantages of the Route-Model. The query performance behaves as expected and increases by approximately one third compared to the Route-Model alone. If we then additionally apply Node-Blocking on the route

Table 2: Comparison of the different models. The Route-Model is computed with $\gamma=5$ for europe and $\gamma=4$ for $b v b$.

| input | Model | Size |  | QUERY |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | \#nodes | \#edges | \#settled [ms] spd-up |  |  |
| europe | Classic expanded | 5,207,980 | 8,505,951 | 1,161,696 | 534.7 | 1.00 |
|  | Phase 1 | 3,472,022 | 6,769,991 | 768,181 | 426.5 | 1.25 |
|  | Phase 2 | 1,736,064 | 15,571,190 | 431,274 | 631.1 | 0.85 |
|  | Route | 5,207,980 | 8,729,619 | 793,462 | 360.6 | 1.48 |
|  | Route w/ blocking | 5,207,980 | 8,729,619 | 313,046 | 154.1 | 3.47 |
|  | Route + Phase 1 | 3,472,018 | 6,821,337 | 439,024 | 256.3 | 2.09 |
|  | Route + Phase $1 \mathrm{w} /$ blocking | 3,472,018 | 6,821,337 | 200,213 | 122.8 | 4.35 |
| $b v b$ | Classic expanded | 2,232,016 | 3,694,253 | 151,379 | 37.6 | 1.00 |
|  | Phase 1 | 1,488,011 | 2,950,248 | 99,253 | 29.1 | 1.29 |
|  | Phase 2 | 744,006 | 13,229,482 | 60,218 | 56.8 | 0.66 |
|  | Route | 2,232,016 | 5,059,228 | 97,978 | 32.6 | 1.15 |
|  | Route w/ blocking | 2,232,016 | 5,059,228 | 63,438 |  | 1.50 |
|  | Route + Phase 1 | 1,488,011 | 3,918,788 | 51,210 |  | 1.66 |
|  | Route + Phase 1 w/ blocking | 1,488,011 | 3,918,788 | 34,032 |  | 2.02 |

+ phase 1 model, we get the best query performance of all the models which yields a speed-up of 4.35 in the railway network of Europe and 2.02 in the Berlin bus network.


### 5.2 Speedup Techniques

Up to now, we showed that by remodeling stations and using additional pruning techniques, we already achieve a speed-up of 4.35 over plain DIJKSTRA. Here, we now show that this approach harmonizes well with other speed-up techniques deriving from road networks.

Path-Selection during Arc-Flags Preprocessing. We already mentioned in Section 4.2 that in expanded timetable networks the number of shortest paths between two nodes is enormously high. It turns out that setting arc-flags for all paths yields a bad query performance. Hence, we have to favor some paths over the others. We proposed four different reasonable strategies: Minimize hops, minimize transfers, minimize accumulated geographic distance along the path and finally minimize the direct geographic distance from the preceding node to the source of the shortest path tree (see Section 4.2). Table 3 shows the impact of each strategy on the performance of Arc-Flags. Note that due to the long preprocessing times of Arc-Flags, we use a subnetwork of our European instance, namely the German railway network called de_fern (6822 stations and 554996 connections).

While minimizing hops is useful in road networks [1] (which can be interpreted there as preferring a route that has less road crossings) this results in a poor performance in railway network. Almost all flags are opened during preprocessing, thus the overhead of the Arc-Flags query algorithm outweighs the benefit from the few remaining pruned arcs. Interestingly, using minimal transfer or minimal distance strategies as

Table 3: Arc-Flags. Evaluation of different path-sepection strategies. For each strategy we apply a partition with 64 cells.

|  | $\left\|\begin{array}{c} \text { PREPRO } \\ {[\mathrm{h}: \mathrm{m}][\mathrm{B} / \mathrm{n}]} \end{array}\right\|$ |  | QUERY <br> \#settled [ms] speed-up |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Strategy |  |  |  |  |  |
| reference | - | 0 | 152,998 | 58.1 | 1.00 |
| hops | 17:00 | 26.2 | 149,931 | 70.3 | 0.83 |
| transfers | 16:26 | 26.2 | 152,307 | 71.7 | 0.81 |
| distance | 20:53 | 26.2 | 134,462 | 61.8 | 0.94 |
| geo. dist. to target | 16:08 | 26.2 | 38,511 | 15.0 | 3.87 |

path selection yields a poor query performance as well. This is mostly due to too many different paths of boundary nodes of the same cell being optimal, thus too many flags are set to true. Recall that the partition is computed on the condensed graph, hence for one station that is at the border of a cell, nodes belonging to all times of day are boundary nodes which may lead to very different transfer or distance minimal routes in the graph.

The minimal direct geographic distance strategy overcomes this issue by always choosing the same preceding node for all times of the day. For that reason, as many arc-flags as possible are kept false, which eventually yields a speed-up of 3.87 on the German railway network. Since all other strategies actually worsen the query performance, we choose the direct geographic distance strategy for further experiments involving Arc-Flags on time expanded railway networks.

Speed-Up Techniques on our Models. In the next experiment we compare the performance of the adapted speed-up techniques on the different models from Section 3. Because of the bad performance of the phase 2 model, we only compare the classic expanded model, the phase 1 model, the Route-Model and the combination of the route and phase 1 models.

Furthermore, we tested the effect of dynamic-landmark-selection against a precomputed set of landmarks. Table 4 shows our results. We show the query performance as well as preprocessing-costs by preprocessing time and additionally bytes per node required to store the preprocessed data. For each model we tested the following speed-up techniques:

- BA: Node-Blocking with ALT.
- BdA: Node-Blocking with ALT and dynamic-landmark-selection.
- uFA: Unidirectional Arc-Flags with ALT.
- uFdA: Unidirectional Arc-Flags with ALT and dynamic-landmark-selection.

Regarding classic ALT we always used a set of 8 precomputed landmarks by the maxCover [9] method. Arc-Flags were computed using a partition of 128 cells obtained from SCOTCH [17]. The strategy for path-selection was geographic distance to target. Note that for Arc-Flags, we turn off Node-Blocking (cf. Section 4.2).

We observe, that for all speed-up technique our modifications to the classic expanded model yield improvements regarding both query performance and preprocessing time. While the transition from the classic to the phase 1 model is more beneficial for

Arc-Flags than ALT with Node-Blocking, the latter performs better on the Route-Model where Node-Blocking fits the model considerably better. The combination "Route + Phase 1" unifies the advantages of each model yielding the best speed-ups.

In general, Arc-Flags has a higher impact on query time than ALT together with Node-Blocking (about 5.5 times faster on both networks) which is being paid for with very high preprocessing time and roughly 30 times more required space per node. Note, that the dynamic ALT comes for free, as it does not require any preprocessing at all. With our modified models we can, however, still achieve a speed-up of 10.13 in Europe and 2.54 in Berlin with dynamic ALT and Node-Blocking, which is useful in a scenario where preprocessing is limited or not allowed.

Table 4: Comparing different models in conjunction with the classic speed-up techniques. The parameter set used throughout: 128 cells, geographic distance to target path-selection-strategy for Arc-Flags and 8 landmarks using maxCover for the classic ALT.

| Model/Algorithm | europe |  |  | $b v b$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { Prepro } \\ & {[\mathrm{h}: \mathrm{m}][\mathrm{B} / \mathrm{n}]} \end{aligned}$ | QUERY |  | $\left\|\begin{array}{c} \text { PREPRO } \\ {[\mathrm{h}: \mathrm{m}][\mathrm{B} / \mathrm{n}]} \end{array}\right\|$ | QUERY |  |  |
|  |  | \#settled | [ms] spd |  | \#settle | [ms] | spd |
| Reference | 0 | 1,161,696 5 | 534.71 .00 | 0 | 151,379 | 37.6 | 1.00 |
| Classic Exp. (BA) | $\approx 4 \mathrm{~s} \quad 4.0$ | 261,151 1 | $\begin{array}{ll}162.7 & 3.29\end{array}$ | $\approx 2 \mathrm{~s} \quad 4.1$ | 96,533 | 33.6 | 1.12 |
| Classic Exp. (BdA) | $\approx 1 \mathrm{~s} \quad 4.0$ | 233,280 1 | 130.84 .09 | $\approx 1 \mathrm{~s} \quad 4.0$ | 94,345 | 29.1 | 1.29 |
| Classic Exp. (uFA) | 106:11 106.5 | 71,937 | 32.716 .35 | 45:30 108.0 | 49,921 | 17.0 | 2.21 |
| Classic Exp. (uFdA) | 106:11 106.5 | 65,143 | 33.915 .77 | 45:30 107.9 | 49,014 | 15.2 | 2.47 |
| Phase 1 (BA) | $\approx 5 \mathrm{~s} 4.5$ | 208,579 | 45.53 .67 | $\approx 2 \mathrm{~s}$ | 67,019 | 26.1 | 1.44 |
| Phase 1 (BdA) | $\approx 1 \mathrm{~s} \quad 4.0$ | 185,996 1 | 116.44 .59 | $\approx 1 \mathrm{~s}$ | 65,488 | 22.8 | 1.65 |
| Phase 1 (uFA) | 77:52 127.2 | 30,583 | 14.038 .19 | 31:59 129.0 | 15,004 | 5.4 | 6.96 |
| Phase 1 (uFdA) | 77:52 126.7 | 27,310 | 18.529 .06 | 31:59 128.9 | 14,713 | 5.1 | 7.37 |
| Route (BA) | $<4 \mathrm{~s} 4.4$ | 140,826 | 73.27 .30 | $\approx 2 \mathrm{~s} 4.1$ | 49,591 | 22.3 | 1.69 |
| Route (BdA) | $\approx 1 \mathrm{~s} \quad 4.0$ | 127,444 | $\begin{array}{ll}65.4 & 8.18\end{array}$ | $\approx 1 \mathrm{~s}$ | 48,390 | 19.8 | 1.90 |
| Route (uFA) | 85:49 109.7 | 50,050 | 22.124 .19 | 50:58 147.1 | 25,289 | 10.2 | 3.69 |
| Route (uFdA) | 85:49 109.3 | 45,180 | 25.321 .13 | 50:58 147.0 | 24,785 | 9.3 | 4.04 |
| Route + Ph. 1 (BA) | $\approx 4 \mathrm{~s} 4.5$ | 89,524 | $\begin{array}{ll}58.7 & 9.11\end{array}$ | $<2 \mathrm{~s} 4.1$ | 26,653 | 16.0 | 2.35 |
| Route + Ph. 1 (BdA) | $\approx 1 \mathrm{~s} \quad 4.0$ | 80,665 | 52.810 .13 | $\approx 1 \mathrm{~s} 4.0$ | 26,007 | 14.8 | 2.54 |
| Route + Ph. 1 (uFA) | 83:58 128.2 | 20,044 | 9.556 .28 | 34:56 170.6 | 6,195 | 2.6 | 4.46 |
| Route + Ph. 1 (uFdA) | 83:58 127.7 | 17,805 | 15.235 .18 | 34:56 170.5\| | 6,053 | 2.8 | 3.43 |

Comparing the standard ALT against ALT with dynamic landmarks, we observe, that regarding query time dynamic ALT only pays off as long as the general speedup (achieved through some other speed-up technique or model) does not exceed the cost we pay for computing the distance table on-the-fly. Since the condensed graph of Europe has about 11 times more stations than the Berlin graph, the cost for computing the dynamic distance table carries much more weight there-A one-to-all DiJKstra takes about 7 ms on the condensed graph of Europe. Hence, it never pays off using dynamic landmarks together with Arc-Flags here. The same effect can be observed in the Berlin network, however, only with the combination of the route and phase 1 models due to the much smaller condensed graph.

Summarizing, our modifications yield a speed-up of 3.5 if we apply ALT and ArcFlags to both time-expanded graphs. The corresponding figure for our bus network is 5.5. This yields an overall speed-up of 56.28 for Europe and 14.46 for Berlin when compared to the classic model without any speed-up technique applied.

### 5.3 Comparison to the Time-Dependent Model

Table 5 compares the performance of DiJKStra's algorithm and ALT applied to our route+phase 1 time-expanded model and the time-dependent model. We observe that by the introduction of our Route-Model (and Node-Blocking) query performance of time-expanded queries are faster than for the time-dependent approach. Hence, we are able to close the performance-gap between both models. Analyzing the time-dependent approach, we notice that Node-Blocking is included implicitly: During a query we do not relax an edge more than once although it represents several connections running from one station to another. Hence, early connections block later ones. Our remodeling and Node-Blocking technique introduces these optimizations to the time-expanded approach. As a result the performance advantage of the time-dependent approach fades.

Table 5: Performance of DijKstraand uni-directional ALT using a time-dependent variant of our European input. For comparison, the corresponding figure for the time-expanded approach (route-model with phase 1) are given as well.

| technique | time-dependent |  |  |  | time-expanded |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Preprotime$[\mathrm{h}: \mathrm{m}]$ | QUERIES |  |  | PREPRO time [h:m] | Queries |  |  |  |
|  |  | \#settled | ed time |  |  | \#settled | peed | tim |  |
|  |  | nodes | up [ms] | up |  | nodes |  | [ms] | up |
| Dijkstra | 0:00 | 260095 | 1.0125 .2 | 1.0 | 0:00 | 200213 |  | 122.8 | 1.0 |
| uni-ALT | 0:02 | 127103 | $2.0 \quad 75.3$ | 1. | 0:01 | 89524 | 2.2 | 258.7 | 2.1 |

## 6 Conclusion

In this work, we introduced a local remodeling routine for the time-expanded approach based on the intuition that at many stations in a network, the number of reasonable choices is little. It turns out that this approach leads to a closely related speed-up technique harmonizing well with our remodeling. Moreover, we adapted speed-up techniques to the time-expanded model and show that they harmonize well with our new approach. Altogether, our approach yields query times up to 56.28 times faster than pure Dijkstra.

Regarding future work, we are optimistic that our approach would also work well for multi-criteria optimization. Although our pruning techniques may not work as strict as for single-criteria search, the number of reasonable choices is little in this scenario as well. Another very important problem is dynamization. It seems as if updating a time-expanded graph is rather expensive, though possible [3, 15].

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