Distributed Computing Meets Game Theory

Fault Tolerance and Implementation with Cheap Talk

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— Abstract -

Traditionally, work in distributed computing has divided the agents into "good guys" and "bad guys". The good guys follow the protocol; the bad guys do everything in their power to make sure it does not work. By way of contrast, game theory has focused on "rational" agents, who try to maximize their utilities. Here I try to combine these viewpoints. Specifically, following the work of Abraham et al. [2], I consider (k,t)-robust protocols/strategies, which tolerate coalitions of rational players of size up to k and up to t malicious players. I focus in particular on the problem that economists have called implementing a mediator. That is, can the players in the system, just talking among themselves (using what economists call "cheap talk") simulate the effects of the mediator (see, e.g., [3, 4, 5, 6, 8, 10, 11]). In computer science, this essentially amounts to multiparty computation [7, 9, 12]. Ideas from cryptography and distributed computing allow us to prove results on how many agents are required to implement a (k,t)-robust mediator just using cheap talk. These results subsume (and, in some cases, correct) results from the game theory literature.

The results of Abraham et al. [2] were proved for what are called $synchronous\ systems$ in the distributed computing community; this is also the case for all the results in the economics literature cited above. In synchronous systems, communication proceeds in atomic rounds, and all messages sent during round r are received by round r+1. But many systems in the real world are asynchronous. In an asynchronous setting, there are no rounds; messages sent by the players may take arbitrarily long to get to their recipients. Markets and the internet are best viewed as asynchronous. Blockchain implementations assume $partial\ synchrony$, where there is an upper bound on how long messages take to arrive. The partial synchronous setting already shows some of the difficulty of moving away from synchrony: An agent i can wait to take its action until it receives a message from j (on which its action can depend). This cannot happen in a synchronous setting. Abraham, Dolev, Geffner, abnd Halpern [1] extend the results on implementing mediators to the asynchronous setting.

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Category Invited Talk

Related Versions The talk described by this paper is based on two papers: "Distributed computing meets game theory: robust mechanisms for rational secret sharing and multiparty computation", by Ittai Abraham, Danny Dolev, Rica Gonen, and Joseph Y. Halpern, which appeared in the *Proceedings of the 25th Annual ACM Symposium on Principles of Distributed Computing*, pp. 53–62, 2006, and "Implementing mediators with asynchronous cheap talk", by Ittai Abraham, Danny Dolev, Ivan Geffner, Joseph Y. Halpern, which appeared in *Proceedings of the 38th Annual ACM Symposium on Principles of Distributed Computing*, pp. 501–510, 2019.

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