# Fishing Fort: A System for Graph Analytics with ML Prediction and Logic Deduction 

Wenfei Fan $\square$ 숭<br>Shenzhen Institute of Computing Sciences, China<br>University of Edinburgh, UK<br>Beihang University, Beijing, China<br>Shuhao Liu $\square$ 수<br>Shenzhen Institute of Computing Sciences, China


#### Abstract

This paper reports Fishing Fort, a graph analytic system developed in response to the following questions. What practical value can we get out of graph analytics? How can we effectively deduce the value from a real-life graph? Where can we get clean graphs to make accurate analyses possible? To answer these questions, Fishing Fort advocates to unify logic deduction and ML prediction by proposing Graph Association Rules (GARs), a class of logic rules in which ML models can be embedded as predicates. It employs GARs to deduce graph associations, enrich graphs and clean graphs. It has been deployed in production lines and proven effective in online recommendation, drug discovery, credit risk assessment, battery manufacturing and cybersecurity, among other things.


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## 1 Introduction

When working with practitioners in industry, we often hear the following questions.
(1) What practical value can we get out of big data analytics? After a decade of study, people are still scrambling to find killer apps of big data analytics. While the success of machine learning (ML) should be at least partly attributed to big data, people have higher expectations from big data analytics to help them solve problems at hand, e.g., optimize a costly step in a manufacturing process or find the use of an old drug for a new disease. Besides, big data analytics gets credits for making an advance only if it is not entirely ML-based, i.e., it approaches the problem not by simply training and applying an ML model.
(2) How should we analyze big data, ML prediction or logic deduction? Data analytics is often approached by employing either ML models or logic rules. However, neither of the two is superior to the other. On the one hand, it is hard to discover a small number of accurate logic rules to cover different cases of our application and data. On the other hand, ML predictions are probabilistic and hard to explain; practitioners may not want to make critical decisions based on ML predictions alone. Is it possible to unify the two and benefit from both?
(3) Where can we get clean data for analytics? Real-life data is often dirty, as evidenced by duplicates, semantic inconsistencies, stale data and missing values commonly found in practice. Dirty data has been a longstanding challenge. To make practical use of big data analytics, it is a must to clean the data. Indeed, data-driven decisions based on dirty data can be worse than making decisions with no data. For instance, "as a healthcare, retail, or financial services business you cannot afford to make decisions based on yesterday's data" [9].

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In an effort to tackle these questions, we have developed Fishing Fort, a system for deducing associations among entities in graphs. Fishing Fort has been deployed in the production lines of several domains, and has proven effective there. The system is named in memory of the siege of Diaoyu (Fishing) Fortress (a.k.a. Diaoyu Castle), a battle during which the fourth khagan of the Mongol Empire was severely wounded to death by the defenders, and a battle that changed the history of China and the world. The system has several unique features.
(1) Unification of $M L$ and logic. Fishing Fort unifies ML prediction and logic deduction by employing a class of Graph Association Rules (GARs) [17]. A GAR is composed of a graph pattern to identify related entities, and a dependency on the entities to disclose their association, correlation and interaction. Taken together, the pattern and dependency reveal regularities among entities in graphs. Moreover, a GAR may embed ML models as predicates. As a consequence, GARs may embed ML predictions in logic deduction, and moreover, explain local predictions of ML models such as graph neural networks (GNNs) [26, 27, 4].
(2) Accurate association deduction. Fishing Fort deduces associations with GARs. It supports algorithms for discovering GARs from real-life graphs [13], conducting (batch and incremental) deduction [17] and making event predictions [18]. It has found successful applications in early drug discovery [11], lithium-ion battery manufacturing, risk control for bank loans, cyber attack detection and online recommendation in e-commerce [10], among other things.
(3) Data enrichment and cleaning. Fishing Fort can also be used to improve the quality of real-life graphs. Given a graph $G$, it enriches $G$ by extracting data that pertains to the entities of $G$ from external data sources, e.g., knowledge graphs [19]. It detects and fixes errors in the (enriched) graph by employing a special form of GARs [12], in polynomial time (PTIME). The fixes computed are logical consequences of the rules and accumulated ground truth (i.e., validated facts); hence if the rules and ground truth are correct, so are the fixes.

Organization. The remainder of the paper is organized as follows. Section 2 defines GARs. Section 3 presents the architecture of Fishing Fort and showcases how it deduces associations with GARs in real-life applications. Section 4 shows how Fishing Fort enriches and cleans graphs with (a special form) of GARs. Finally, Section 5 discusses future plans.

## 2 Unifying ML prediction and Logic Deduction

This section reviews basic notations (Section 2.1), and defines Graph Association Rules (GARs) (Section 2.2). It also reports the complexity for reasoning about GARs (Section 2.3).

### 2.1 Preliminaries

Assume three countably infinite sets of symbols, denoted by $\Omega, \Upsilon$ and $U$, for labels, attributes and constants, respectively. We consider graphs $G=\left(V, E, L, F_{A}\right)$, where (a) $V$ is a finite set of vertices, (b) $E \subseteq V \times \Omega \times V$ is a finite set of edges, where each $e=\left(v, l, v^{\prime}\right)$ in $E$ denotes an edge from vertex $v$ to $v^{\prime}$ that is labeled with $l \in \Omega$, (c) $L$ is a function such that for each vertex $v \in V, L(v)$ is a label from $\Omega$, and (d) each vertex $v \in V$ carries a tuple $F_{A}(v)=\left(A_{1}=a_{1}, \ldots, A_{n}=a_{n}\right)$ of attributes of a finite arity, where $A_{i} \in \Upsilon$ and $a_{i} \in U$, written as $v . A_{i}=a_{i}$, and $A_{i} \neq A_{j}$ if $i \neq j$, representing properties. Different vertices may carry different attributes, which are not constrained by a schema.

A graph pattern is $Q[\bar{x}]=\left(V_{Q}, E_{Q}, L_{Q}, \mu\right)$, where (1) $V_{Q}$ (resp. $E_{Q}$ ) is a finite set of pattern nodes (resp. edges), (2) $L_{Q}$ assigns a label $L_{Q}(u) \in \Gamma$ to each pattern node $u \in V_{Q}$, (3) $\bar{x}$ is a list of distinct variables; and $\mu$ is a mapping that assigns a distinct variable to each node $v$ in $V_{Q}$. For $x \in \bar{x}$, we use $\mu(x)$ and $x$ interchangeably when it is clear in the context.

A match of pattern $Q[\bar{x}]$ in graph $G$ is defined as a homomorphism $h$ from $Q$ to $G$ such that (a) for each node $u \in V_{Q}, L_{Q}(u)=L(h(u))$; and (b) for each pattern edge $e=\left(u, l, u^{\prime}\right)$ in $Q, e^{\prime}=\left(h(u), l, h\left(u^{\prime}\right)\right)$ is an edge in $G$. We denote the match as a vector $h(\bar{x})$, consisting of $h(x)$ for all $x \in \bar{x}$ in the same order as $\bar{x}$, denoting entities identified by $Q$.

### 2.2 Graph Association Rules

GARs are defined with predicates. A predicate of pattern $Q[\bar{x}]$ is one of the following:

$$
p::=l(x, y)|x \cdot A \otimes y \cdot B| x \cdot A \otimes c \mid \mathcal{M}(x \cdot \bar{A}, y \cdot \bar{B})
$$

where $\otimes$ is one of $=, \neq,<, \leq,>, \geq ; l \in \Omega ; x$ and $y$ are variables in $\bar{x} ; c$ is a constant in $U ; A$ and $B$ are attributes; and $x \cdot \bar{A}$ is a list of attributes at "vertex" $x$; similarly for $y \cdot \bar{B}$.

The predicates are classified as follows. (1) Logic predicates: link predicate $l(x, y)$ indicates the existence of an edge labeled $l$ from vertex $x$ to $y$; variable predicate $x . A \otimes y . B$ and constant predicate $x . A \otimes c$ check the correlation and interaction of attribute values. (2) ML predicates: $\mathcal{M}(x . \bar{A}, y \cdot \bar{B})$ is a pre-trained ML model that returns true iff $\mathcal{M}$ predicts true at $(x . \bar{A}, y \cdot \bar{B})$. Here $\mathcal{M}$ can be any ML model that returns Boolean (e.g., $\mathcal{M} \geq \sigma$ for a predefined bound $\sigma$ ).

Rules. A GAR (Graph Association Rule) is a pair of a graph pattern and a dependency [17]:

$$
\varphi=Q[\bar{x}]\left(X \rightarrow p_{0}\right),
$$

where $Q[\bar{x}]$ is a graph pattern, $X$ is a conjunction of predicates of $Q[\bar{x}]$, and $p_{0}$ is a single predicate of $Q[\bar{x}]$. We refer to $Q[\bar{x}]$ and $X \rightarrow p_{0}$ as the pattern and dependency of GAR $\varphi$, respectively, and to $X$ and $p_{0}$ as the precondition and consequence of $\varphi$, respectively.

Intuitively, $Q$ in a GAR identifies entities in a graph, and $X \rightarrow p_{0}$ is applied to the entities. Predicates $x . A \otimes c$ and $x . A \otimes y . B$ specify value associations of attributes. Link predicates enforce edge existence to deduce missing links. Moreover, one can "plug in" pre-trained ML models $\mathcal{M}$ for entity resolution [33], link predictions [44] and similarity checking [8]. For each application domain, Fishing Fort maintains a library of pre-trained ML models.

We can uniformly express various ML models we used as link prediction for $l(x, y)$, where the label $l$ can indicate (1) a predicted link, (2) the match of $x$ and $y$ as the same entity, linked by a dummy edge with " $=$ " as $l$, or (3) semantic similarity between vertices $x$ and $y$ linked by an edge with " $\approx$ " as $l$, indicating that $x$ and $y$ are "semantically" close.

We will showcase GARs for real-life applications in Section 3.
As shown in [17], graph functional dependencies (GFDs) [23], graph entity dependencies (GEDs) [20] and graph pattern association rules (GPARs) [22] are special cases of GARs. GARs extend these graph dependencies by supporting ML and link predicates. Note that link predicates mutate the topological structure of a graph. Besides the primitive predicates above, Fishing Fort also supports, e.g., local 2-dimensional Weisfeiler-Leman (local 2-WL) test [27], to explain GNN-based recommendations and link predictions. It is known that such GNN models are no more expressive than local 2-WL test [27].

Semantics. Consider a $\operatorname{GAR} \varphi=Q[\bar{x}]\left(X \rightarrow p_{0}\right)$. Denote by $h(\bar{x})$ a match of pattern $Q$ in a graph $G$, and by $p$ a predicate of $Q[\bar{x}]$. We write $h(\mu(x))$ as $h(x)$, where $\mu$ is the mapping in $Q$ from $\bar{x}$ to vertices in $Q$. A match $h(\bar{x})$ satisfies a predicate $p$, denoted by $h(\bar{x}) \models p$, if one of following conditions is satisfied: (a) when $p$ is $l(x, y)$, there exists an edge with label $l$ from $h(x)$ to $h(y) ;(\mathrm{b})$ when $p$ is $x . A \otimes y . B$, the vertex $h(x)$ (resp. $h(y))$ carries attribute $A$ (resp. $B$ ), and $h(x) \cdot A \otimes h(y) \cdot B$; similarly for constant predicate $h(x) . A \otimes c$; and (c) when $p$ is $\mathcal{M}(x . \bar{A}, y \cdot \bar{B})$, the ML model $\mathcal{M}$ predicts true at $(h(x) . \bar{A}, h(y) \cdot \bar{B})$.

We write $h(\bar{x}) \models X$ if $h(\bar{x}) \models p$ for all $p$ in a set $X$ of predicates. We write $h(\bar{x}) \models$ $X \rightarrow p_{0}$ if whenever $h(\bar{x}) \models X$, then $h(\bar{x}) \models p_{0}$. We say that a graph $G$ satisfies GAR $\varphi=Q[\bar{x}]\left(X \rightarrow p_{0}\right)$, denoted by $G \models \varphi$, if for all matches $h(\bar{x})$ of $Q[\bar{x}]$ in $G, h(\bar{x}) \models X \rightarrow p_{0}$. We say that $G$ satisfies a set $\Sigma$ of GARs, denoted by $G \models \Sigma$, if for all GARs $\varphi \in \Sigma, G \models \varphi$.

For $p=x . A \otimes c$, we use $h(p)$ to denote $h(x) . A \otimes c$; similarly for the other predicates. For a set $X$ of predicates, we denote by $h(X)$ the collection of $h(p)$ for all $p$ in $X$. For a set $\Gamma$ of validated facts of the forms $u . A \otimes v . B$ and $u . A \otimes c$ for vertices $u, v$ in a graph $G$, we say that $h(p)$ is validated with $\Gamma$ if it is enclosed in $\Gamma$; in particular, for $p=\mathcal{M}(x . \bar{A}, y \cdot \bar{B})$, the values of $h(x) . A$ and $h(y) . B$ are enclosed in $\Gamma$ for all corresponding $A \in \bar{A}$ and $B \in \bar{B}$; similarly for $h(X)$. As will be seen in Section 3.1, we check validated facts to deduce reliable associations.

### 2.3 Complexity

There are three classical problems for dependencies, stated as follows.
The satisfiability problem is to decide, given a set $\Sigma$ of GARs, whether there exists a graph $G$ such that $G \models \Sigma$ and for each $\operatorname{GAR} Q[\bar{x}]\left(X \rightarrow p_{0}\right) \in \Sigma, Q$ has a match in $G$ ? Intuitively, this is to ensure that all GARs can be applied to $G$ at the same time without conflicts.

A set $\Sigma$ of GARs implies a GAR $\varphi$, denoted by $\Sigma \models \varphi$, if for all graphs $G$, if $G \models \Sigma$ then $G \models \varphi$, i.e., $\varphi$ is a logical consequence of $\Sigma$. The implication problem is to decide, given a set $\Sigma$ of GARs and a GAR $\varphi$, whether $\Sigma \models \varphi$ ? Intuitively, the implication analysis can help us remove redundant GARs in rule discovery and speed up association analyses with GARs.

The validation problem is to decide, given a graph $G$ and a set $\Sigma$ of GARs, whether $G \models \Sigma$ ? Intuitively, this is to settle the complexity of association analyses with GARs.

To simplify the implication analysis, we consider ML predicates of the form $\mathcal{M}(x \cdot \bar{A}, y \cdot \bar{B}) \geq$ $\sigma$ for a predefined $\sigma$. Moreover, we assume that the ML models in a set of GARs are independent, i.e., they are trained for different purposes and do not overlap/entail each other, e.g., models for predicting the anomaly and capacity of battery cells in battery manufacturing.

It has been shown that the satisfiability, implication and validation are coNP-complete, NP-complete, and coNP-complete for GARs, respectively [17, 20]. Here we assume that given two lists of attributes $x . \bar{A}$ and $y \cdot \bar{B}$, checking $\mathcal{M}(x . \bar{A}, y \cdot \bar{B})$ is in PTIME in the sizes $|x . \bar{A}|$ and $|y \cdot \bar{B}|$, as commonly found in practice for pre-trained $\mathcal{M}$. The complexity bounds are the same as for reasoning about GEDs [20]. Moreover, the implication and satisfiability analyses are no harder than their counterparts for relational conditional functional dependencies [14].

## 3 Deducing Graph Associations

This section first presents the architecture and workflow of Fishing Fort (Section 3.1), and then showcases its applications in different domains (Section 3.2).

### 3.1 The Architecture of Fishing Fort

As shown in Figure 1, Fishing Fort supports both association deduction, and graph enrichment and cleaning. For each application domain, it maintains a set $\Gamma$ of ground truth, and references relevant external knowledge graphs KG. Given a real-life graph $G$, it first enriches $G$ by extracting relevant data from KG and cleans the enriched $G$; to simplify the discussion, we refer to the enriched and cleaned graph also as $G$. After the preprocessing step, Fishing Fort then discovers a set $\Sigma$ of GARs for the application, and deduces associations from $G$ with the GARs of $\Sigma$; in the process it accumulates ground truth for subsequent analyses. Below we focus on association deduction, and defer data enrichment and cleaning to Section 4.

Association deduction is carried out by the following main modules and algorithms.


Figure 1 The architecture of Fishing Fort.

Rule discovery. Fishing Fort implements the parallel algorithm of [13] for discovering GARs. To scale with a large graph $G$, it employs three strategies. (1) Application-driven discovery. Given an application $\mathcal{A}$, Fishing Fort trains an ML model $\mathcal{M}_{\mathcal{A}}$ to identify vertices, edges and properties in $G$ that pertain to $\mathcal{A}$. It reduces $G$ to a smaller graph $G_{\mathcal{A}}$ that consists only of the data pertaining to $\mathcal{A}$. Moreover, it discovers $\mathcal{A}$-relevant rules, i.e., GARs with consequence predicates selected by $\mathcal{M}_{\mathcal{A}}$. (2) Sampling. It samples a set $H$ of graphs from $G_{\mathcal{A}}$ such that each graph is at most $\rho \%$ of $G_{\mathcal{A}}$ and consists of representative entities in $G_{\mathcal{A}}$ and their surrounding subgraphs, for a predefined bound $\rho \%$. Denote by $\Sigma_{G}$ and $\Sigma_{H}$ the set of $\mathcal{A}$-relevant rules discovered from $G$ and $H$, respectively. Fishing Fort guarantees that given bounds $\sigma$ and $\gamma \%$, it samples $H$ such that (a) at least $\gamma \%$ of rules in $\Sigma_{G}$ are covered by $\Sigma_{H}$, and (b) each of these rules can be applied at least $\sigma$ times on the entire $G$, i.e., the rules in $\Sigma_{H}$ have recall above $\gamma \%$ and support above $\sigma$ over the original graph $G$. (3) Parallel scalability. Fishing Fort employs data-partitioned parallelism. It partitions $G$ and distributes the fragments across different machines. It works on the fragments in parallel and guarantees to reduce runtime when more machines are used, i.e., the parallel scalability [29]. Hence in principle, it can scale with large graphs $G$ by using more machines when needed.

Association deduction. Fishing Fort deduces link and value associations from graph $G$, by chasing $G$ with the set $\Sigma=\Sigma_{H}$ of GARs discovered. More specifically, it applies a GAR $Q[\bar{x}]\left(X \rightarrow p_{0}\right)$ to $G$ only if there exists a match $h$ of $Q$ in $G$ such that $h \models X$ and the $h(X)$ is validated with the ground truth in $\Gamma$ (see Section 2.2); if so, it deduces association $h\left(p_{0}\right)$ and adds $h\left(p_{0}\right)$ to $\Gamma$ as validated facts for subsequent deduction. To carry this out, it implements a combination of the parallel algorithms of [17, 21], and supports two modes: (1) batch mode, to deduce all associations from $G$ at once, and (2) incremental mode, to deduce changes online to associations in response to updates to $G$. In both modes, users may also opt to pick entities of their interest and deduce associations pertaining to these entities only. Moreover, it explains ML predictions if requested by users (see Section 3.2.1).

Fishing Fort provides the following performance guarantees. (a) The chase is ChurchRosser [1], i.e., it guarantees to terminate and converge at the same result no matter what GARs in $\Sigma$ are used and in what order the rules are applied. (b) The deduced associations are logical consequences of the GARs of $\Sigma$ and ground truth of $\Gamma$; hence if $\Sigma$ and $\Gamma$ are correct, so are the deduced associations. (c) Its deduction algorithm is also parallelly scalable.

Implementation. Fishing Fort is implemented on top of GRAPE [24], a graph engine that parallelizes single-machine graph algorithms based on a fixpoint model in terms of partial evaluation and incremental computation. GRAPE was acquired by Alibaba Group and renamed as GraphScope [16]; it supports $90+\%$ of daily graph computations of Alibaba.

### 3.2 Fishing Fort in Action

We next present example applications of Fishing Fort, along with GARs discovered from real-life data. The graph patterns of the GARs are depicted in Figure 2.

### 3.2.1 Online Recommendation

ML models have been widely used in e-commerce to recommend items to users. The models are often classified as collaborative filtering (CF) and content-based (CB). CF identifies user preference and makes recommendation by learning from user-item historical interactions, e.g., users' previous ratings and browsing history, and CB primarily compares the contents of users and items such as user profiles and item features. However, a single strategy, either CF or CB, often does not suffice in practice. For example, instead of exploring new interesting items, CF tends to find similar ones w.r.t. the user's past interaction due to its collaborative nature. It does not work well when the interaction data is sparse and when a recommender system starts cold. To rectify these limitations, hybrid models have been explored to unify interaction-level similarity and content-level similarity. However, the hybrid approach often requires training a new ML model starting from scratch. Moreover, the ML models usually compute a prediction score, i.e., recommendation strength, between each user $x$ and item $y$, and recommend $y$ to $x$ only if the score is above some predetermined thresholds. As a result, these ML models often make false positive (FP) or false negative (FN) predictions, especially in the "fuzzy area" where the predicted scores are near the thresholds, i.e., an area where the prediction strengths are neither sufficiently large nor sufficiently small.

Another issue concerns the explanation of ML predictions $\mathcal{M}(x, y)$, to tell why an item $y$ is recommended to user $x$. The need for this is twofold, (a) to provide the users with insights and establish their trust in the predictions, and (b) help developers debug ML models by revealing errors or bias in training data that result in adverse and unexpected behaviors.

Fishing Fort has been deployed at e-commerce companies to reduce FPs and FNs of ML recommendation models, and provide local explanations of GNN-based recommendations. It improves the average click-through rate of the companies by up to $50 \times$.
(a) Reducing FPs and FNs of ML predictions. Consider an ML model $\mathcal{M}_{\text {rate }}(x, y)$ for movie recommendations that, given a movie $y$ and a user $x$, outputs a numeric score, i.e., recommendation strength, between $(0,1)$. The higher the score, the stronger the confidence. Take 0.5 as the strength threshold, i.e., $\mathcal{M}_{\text {rate }}$ recommends $y$ to $x$ if $\mathcal{M}_{\text {rate }}(x, y) \geq 0.5$.

As an example, $\operatorname{GAR} \varphi_{1}=Q_{1}[\bar{x}]\left(X_{1} \wedge 0.5 \leq \mathcal{M}_{\text {rate }}\left(x_{0}, x_{1}\right) \leq 0.6 \rightarrow\right.$ dislike $\left.\left(x_{0}, x_{1}\right)\right)$ corrects some FPs of ML model $\mathcal{M}_{\text {rate }}$ in its "fuzzy area" of recommendations. Together with $Q_{1}$, precondition $X_{1}$ specifies the following: (1) user $x_{0}$ disliked a high-rating movie $x_{2}$, which stars the same actor $x_{4}$ as movie $x_{1}$ does; and (2) $x_{0}$ also disliked another high-rating movie $x_{3}$, which is directed by the director $x_{5}$ of movie $x_{1}$. Intuitively, model $\mathcal{M}_{\text {rate }}$ (especially if it is CF-based) is inclined to make the recommendation of movie $x_{1}$ to user $x_{0}$, since many other users could have positive interactions with movies $x_{1}, x_{2}$ and $x_{3}$ (hence the high ratings). However, GAR $\varphi_{1}$ overrides the prediction with logic conditions $X_{1}$, because unlike an average user, user $x_{0}$ seems to approve neither the leading actor nor the director of movie $x_{1}$. Among the matching cases of $Q_{1}$ in real-world datasets, this rule reduces FPs by $92.3 \%$.


Figure 2 Graph patterns in real-life GARs.

In contrast, GAR $\varphi_{2}=Q_{2}[\bar{x}]\left(X_{2} \wedge 0.4 \leq \mathcal{M}_{\text {rate }}\left(x_{0}, x_{1}\right) \leq 0.5 \rightarrow\right.$ like $\left.\left(x_{0}, x_{1}\right)\right)$ suggests recommending a war movie $x_{1}$ to user $x_{0}$ regardless of the negative ruling of $\mathcal{M}_{\text {rate }}\left(x_{0}, x_{1}\right)$, if the following conditions ( $Q_{2}$ and $X_{2}$ ) are met: (1) $x_{0}$ disliked a war movie $x_{4}$, yet (2) $x_{0}$ liked a musical $x_{3}$ directed by $x_{2}$, the director of movie $x_{1}$. Model $\mathcal{M}_{\text {rate }}$ may infer that $x_{0}$ is not a fan of war movies based on the interaction with $x_{4}$. Nonetheless, rule $\varphi_{2}$ rejects the prediction, based on the evidence that $x_{0}$ is likely a fan of director $x_{2}$. Over verification datasets, GAR $\varphi_{2}$ reduces FNs of $\mathcal{M}_{\text {rate }}$ by $87 \%$ for the matching cases of "fuzzy" predictions.
(b) Explaining ML predictions. Consider $\varphi_{3}=Q_{3}[\bar{x}]\left(X_{3} \rightarrow \mathcal{M}_{\text {rec }}\left(x_{0}, x_{6}\right)\right)$, where $\mathcal{M}_{\text {rec }}$ is a GNN-based model, $\mathcal{M}_{\text {rec }}\left(x_{0}, x_{6}\right)$ indicates that the model recommends movie $x_{6}$ to user $x_{0}$, and $X_{3}$ is $x_{0}$.age $\geq 18 \wedge x_{0}$.age $<25 \wedge x_{2}$.rating $\geq 6 \wedge x_{3}$.genre $=$ "Action" $\wedge x_{6}$.genre $=$ "Action" $\wedge x_{6}$.year $\geq 2020 \wedge x_{5}$.type $=$ "Academy Award". As opposed to the previous rules, the consequence predicate of this GAR is an ML predicate. Fishing Fort discovers pattern $Q_{3}$ and precondition $X_{3}$ to explain $\mathcal{M}_{\text {rec }}$ predictions from the movie-watching history and friendship of $x_{0}$, and highlights important features of $x_{0}$ and $x_{6}$.

As a concrete example, suppose that the GNN model $\mathcal{M}_{\text {rec }}$ recommends a movie $y_{0}$ "Everything Everywhere All at Once" to a user $x_{0}$ "Mike". Then $\varphi_{3}$ may provide high-level rationale behind the recommendation as follows: the movie is recommended to Mike because Mike is a young adult and has watched action movies before, the movie won the 95th academy award for best picture, and it is directed by "Daniel Scheinert", the director of a favorite movie of a friend Peter of Mike. This provides a local explanation of the prediction.

Unlike previous methods for explaining ML predictions, e.g., SubgraphX [47] and GNNExplainer [46], Fishing Fort not only provides a subgraph as an explanation, but also tells us what features are decisive for an ML model to make predictions and under what conditions the predictions can be made. Moreover, Fishing Fort supports a predicate of local 2-WL test, and therefore, is able to explain common GNN-based recommendations, which is no more expressive than local 2-WL test [27]. In this way, Fishing Fort deduces local explanations for individual instances with GARs. Moreover, the rules for a GNN-based recommendation model $\mathcal{M}$ disclose the general behaviors of $\mathcal{M}$ and can serve as global explanations of $\mathcal{M}$.

### 3.2.2 Early Drug Discovery

Drug discovery is the process of new drug identification, which starts from target selection and validation, through preclinical screening, to clinical trials [25]. It is time-consuming and quite expensive. The development of a new drug takes $10-15$ years, costs around 2 billion US dollars, and typically has a high risk of failure ( $>90 \%$ ) [50].

To accelerate drug discovery, reduce the cost, and increase the success rate, ML models have been explored to identify drug-disease associations (DDAs), drug-drug interactions (DDIs), and protein-protein interactions (PPIs). However, it is costly to train deep-learning models for accurate predictions, and the predictions often have false positives and false negatives. Moreover, ML predictions "still lack reliable explanations that are crucial to drug repurposing and ADR (adverse drug reaction)" [50]. Worse still, noise is often introduced by "unavoidable inaccuracy" of the ML models, e.g., nonexistent relations and inaccurately named entities. Add to the complication that the models are often trained on possibly dirty data, especially when the data comes from multiple sources.

Fishing Fort has been adopted in the early stage of drug discovery. It is used to assist (1) target identification, to identify the right biological molecules or cellular pathways that can be modulated by drugs to achieve therapeutic benefits, where PPIs are often crucial, (b) drug repurposing, to reuse existing drugs for a new disease, and (c) ADR, to disclose undesirable impacts that do not meet the anticipated therapeutic effects and may cause injuries to patients. The need for these is evident. For example, target identification is perhaps the most crucial initial step in drug discovery, and influences the chances of success at every step of drug development. Traditional target identification usually starts in an academic setting, and takes from years to decades. Fishing Fort helps select candidate targets and speed up the process. It identifies DDAs, DDIs and PPIs simply as missing links. Moreover, it has been used to integrate and clean biomedical libraries and data banks (see Section 4).

As an example, Fishing Fort was used to discover GARs for repositioning of existing drugs that may have therapeutic effect on a particular type of Parkinson disease. A GAR is $\varphi_{4}=Q_{4}[\bar{x}]\left(X_{4} \rightarrow l\left(x_{0}, x_{1}\right)\right)$. Together with $Q_{4}$, precondition $X_{1}$ specifies the following: (1) drug $x_{0}$ has a known effect on an inborn genetic blood disease $x_{2}$; (2) disease $x_{1}$ is the Parkinson; (3) drug $x_{0}$ interacts with a gene $x_{3}$, which shares an effect pathway $x_{4}$ with $x_{1}$; (4) drug $x_{0}$ can interact with a gene $x_{5}$, which has an $\mathcal{M}_{\text {drug }}$-predicted relationship with $x_{1}$ (the dashed arrow in $Q_{4}$ ), where $\mathcal{M}_{\text {drug }}$ is a pre-trained ML model that predicts the associations between genes and diseases [40, 34, 44]; and (5) drug $x_{0}$ has a known effect on a type of skin cancer $x_{6}$, which shares an effect pathway with $x_{1}$. The predicted link $l\left(x_{0}, x_{1}\right)$ (the bold line in $Q_{4}$ ) indicates that drug $x_{0}$ may have impact on Parkinson $x_{1}$ in some way.

Such GARs suggest five drugs that may have a hidden association with the particular type of Parkinson's disease, including Colforsin (Forskolin) [53], Sulindac [36, 6], Tamoxifen [32], and Tretinoin [43]. Our partners in pharmacy have verified four predictions with published evidence. The remaining one is undergoing their active lab investigation.

As another example, Fishing Fort discovered GARs for PPIs. Such a GAR is $\varphi_{5}=$ $Q_{5}[\bar{x}]\left(\mathcal{M}_{\mathrm{ppi}}\left(x_{0}, x_{0}\right) \geq \delta \wedge X_{5} \rightarrow l\left(x_{0}, x_{0}\right)\right)$, in which $\mathcal{M}_{\mathrm{ppi}}$ is an RGCN model [37] that predicts PPIs, $\delta$ is a prediction threshold, where each vertex in $Q_{5}$ denotes a protein and each edge denotes a known PPI, and $X_{5}$ specifies additional logic conditions e.g., the domains and subcellular locations, on proteins in $Q_{5}$. This GAR identifies the self-interaction $l\left(x_{0}, x_{0}\right)$ on $x_{0}$. It has found a self-interaction on protein SYT2 (the bold line in $Q_{5}$ ) in May 2022, which coincides the finding published in Nature in the same month [31].

When the consequence $p_{0}$ of a GAR is an ML model for DDA, DDI or PPI, Fishing Fort can discover pattern $Q$ and conditions $X$ to explain the ML prediction, along the same lines as what we have shown in Section 3.2.1 for local explanations of online recommendation.

### 3.2.3 Credit Risk Assessment in Banking

Credit risk assessment is crucial for a bank in making decisions on applications for loans. It is the process of evaluating the likelihood that a borrower will default on a loan obligation. It helps minimize the risk of loss from defaults while also making credit available to qualified borrowers, thereby ensuring the bank's profitability and long-term sustainability.

In practice, a bank can use credit scoring models to rate borrowers based on their personal financial information, e.g., credit history, cash flows, and debt levels. In addition, it is equally important to look for other indicators, e.g., the borrower's social interactions, which may expose risks in financial health and the potential inability to repay a loan. However, this requires extensive labor from human experts. One of our FinTech partners employs a team of $1,000+$ data analysts, dedicated to disclosing such hidden indicators.

Fishing Fort provides an automated and comprehensive approach. Better yet, it produces indicators that are highly explainable. On graphs $G$ that model user/account interactions, Fishing Fort mined various GARs to assess user risks. A discovered GAR is $\varphi_{6}=Q_{6}[\bar{x}]$ ( $X_{6} \wedge$ $\mathcal{M}_{\text {risk }}\left(x_{0}\right)=$ low $\rightarrow x_{0}$.risk $=$ true $)$, where $\mathcal{M}_{\text {risk }}(x)$ is a credit scoring model that evaluates user $x$ 's default risk as either low, moderate or high, and $X_{6}$ is the conjunction of the following conditions: (1) a new user $x_{0}$ is referred by user $x_{1}$, who failed to repay a loan $x_{2}$; and (2) $x_{0}$ and $x_{1}$ shared a device $x_{3}$ for online banking. The rule suggests that user $x_{0}$ is likely a high-risk borrower if both pattern $Q_{6}$ and precondition $X_{6}$ are satisfied, despite the low-risk prediction made by model $\mathcal{M}_{\text {risk }}$. Intuitively, by taking into account clear evidence of straw borrowing, GAR $\varphi_{6}$ corrects some false negatives of $\mathcal{M}_{\text {risk }}$ predictions.

Another GAR $\varphi_{7}=Q_{7}[\bar{x}]\left(X_{7} \rightarrow x_{0}\right.$. risk $=$ true $)$ states that user $x_{0}$ is likely to default on a loan if $x_{0}$ meets the following conditions specified by pattern $Q_{7}$ and precondition $X_{7}$ : (1) $x_{0}$ over-drafted bank account $x_{1}$ multiple times within the past year; (2) $x_{0}$ owns a car $x_{2}$ that is $20+$ years old; and (3) $x_{0}$ is paying only minimum, compulsory liability insurance $x_{3}$ for the car. It would be difficult for a human expert to discover such a strong indicator of default risk, since any single factor alone constitutes a mere weak association.

Our partner in personal banking has verified the effectiveness of the GARs mined by Fishing Fort over real-world borrower data. Both $\varphi_{6}$ and $\varphi_{7}$ have a lift over 3, whereas the average lift of an expert-written rule is 2 . These rules have been deployed at several banks because of their competitive performance in identifying high-risk borrowers.

### 3.2.4 Lithium-ion Battery Manufacturing

An electric vehicle (EV) battery pack consists of thousands of lithium-ion cells. These cells must have a balanced capacity, since imbalanced cells may reduce EV range and lead to safety issues such as thermal runaway. An essential phase in the battery manufacturing process consists of two steps: (a) battery formation, which activates a cell by performing the initial charge/discharge operation (to form special electrochemical solid electrolyte interphase at the electrode), followed by battery standing (to stabilize the voltage and cool off); and (b) battery grading, to fully discharge/recharge the cell and test its capacity. This phase is costly, taking from 14 to $20+$ hours at different production lines in the industry, and demands specialized devices. It is energy-consuming; per estimation in [48], reducing the battery charge energy by half can save the production line $\$ 65,000$ per GWh capacity (assuming a price of $\$ 0.13 / \mathrm{kWh})$. It accounts for more than one third of the total cost of the Lithium-ion battery cell manufacturing process, and is considered one of the bottlenecks that hinders battery manufacturers from increasing output and reducing the total cost of battery production. Therefore, the Battery Formation and Grading System Market has been singled out as a specialized industry segment [30]. It is crucial for the entire Lithium-ion battery industry, including batteries for EVs, electronics and energy storage, among other things.

Fishing Fort provides a cost-effective solution. Traditionally the formation stage first activates the cell by charging it to a ratio of capacity and then cooling it off for a period of time. Grading then fully discharges it, recharges it to its maximum capacity, and discharges it again at a specific rate. It categorizes the capacity of the cell and its performance based on its individual characteristics. As opposed to full discharge/recharge in the traditional process, Fishing Fort only partially charges/discharges a cell. For example, it charges the cell to $50 \%$ in the formation stage to activate the cell, and collects data in the process; it then either grades the cell based on the data without discharging/recharging it, or fully discharges it and then partially charges it to a certain voltage for grading, to improve the accuracy. By analyzing the data together with data collected from earlier stages prior to formation, Fishing Fort can accurately grade the capacity of the cell and moreover, determine whether the cell is anomalous or not.

To this end, Fishing Fort first discretizes the time-series measurements; it splits the entire process into consecutive procedures based on their charging/discharging current. It models the data as a graph $G$ with three types of vertices: (1) Procedure carries an array of attributes including the procedure ID, its initial/final weights, the initial/final battery state statistics, and the charging/discharging current; (2) State denotes a state in $\mathcal{S}$; and (3) Battery carries metadata of a battery cell, e.g., the cell ID, the testing slot ID, and its capacity interval. An edge denotes a transition between procedures, an association between a battery cell and a procedure (with range constraints), or an edge between a procedure and a state.

On such a graph $G$, Fishing Fort discovered GARs for capacity grading. A (simplified) GAR is $\varphi_{8}=Q_{8}[\bar{x}]\left(X_{8} \rightarrow x_{0}\right.$.capacity $\left.=8\right)$, where its consequence grades a matching battery cell as Capacity Interval 8. Together with $Q_{8}, X_{8}$ specifies the following conditions: (1) the weight before and after the Electrolyte Filling procedure $\left(x_{1}\right)$ is $555 \pm 25 \mathrm{~g}$ and $605 \pm 25 \mathrm{~g}$, respectively; (2) its Formation-A procedure ( $x_{2}$ ) uses a constant charging current at 3.8 A , with initial voltage between $0-100 \mathrm{mV}$ and a final state $324\left(x_{4}\right)$ categorized by $\mathcal{M}_{\text {state }}$ (dashed arrows in $Q_{8}$ ); and (3) its Formation-B procedure ( $x_{3}$ ) uses a constant charging current at 8.8 A , with initial voltage between $3.3-3.4 \mathrm{~V}$ and final state $738\left(x_{5}\right)$. Intuitively, this rule grades the capacity of a battery cell based on the data collected from partial charge/discharge and from prior stages. It does not require full charge/discharge for the grading step.

In real production, about $3 \%$ of the cells have abnormal capacity and thus, should not be packed and assembled with other cells. Fishing Fort also detects anomalous cells online with GARs. It trains an ML model $\mathcal{M}_{a}$, a binary classification model based on LightGBM for detecting anomaly [28]. It embeds $\mathcal{M}_{a}$ in the GARs as a predicate, and filters false positives and false negatives of the predictions of $\mathcal{M}_{a}$ by adding logic predicates to the precondition $X$. Such a (simplified) GAR is $\varphi_{8}^{\prime}=Q_{8}^{\prime}[\bar{x}]\left(x_{1} \cdot \mathrm{pt}_{10} \leq 1.9 \wedge x_{1} \cdot \mathrm{pt}_{14} \geq 86 \wedge \mathcal{M}_{\mathrm{a}}\left(x_{1}\right)=\right.$ false $\rightarrow$ $x_{0}$.status $=$ anomalous), where pattern $Q_{8}^{\prime}$ is similar to $Q_{8}$ but does not contain vertices of State, and $x_{1} \cdot \mathrm{pt}_{10}$ and $x_{1} \cdot \mathrm{pt}_{14}$ are the values of the voltage and the temperature of cell $x_{0}$, respectively. GAR $\varphi_{8}^{\prime}$ overrides the incorrect negative rulings of model $\mathcal{M}_{\mathrm{a}}$ by directly considering erratic measurements, thus effectively reducing the FNs of $\mathcal{M}_{\mathrm{a}}$.

With such GARs, Fishing Fort reduces charging to $35-50 \%$ of the full battery capacity, $75-$ $100 \%$ of discharge (in some cases it avoids the grading step completely), and the time for the capacity grading process from 14 hours to 4 hours. With the data of partial charge/discharge, it keeps the error rate under $0.4 \%$, a record in the industry. These translate to an $80 \%$ reduction in energy consumption for charging and cooling, cutting equipment costs by half.

### 3.2.5 Cyber Attack Detection

Cyber attack detection is increasingly vital to enterprise cybersecurity. It aims to identify, analyze, and mitigate threats that could compromise the integrity, confidentiality, and availability of a network. To this end, a common practice is to employ various specialized
hardware devices for threat detection and prevention, while ensuring compliance with security standards and regulations. For example, an enterprise network may deploy multiple instances of (a) Web Application Firewalls (WAF), which monitor, filter and block malicious traffic to and from a Web application, and (b) Intrusion Prevention Systems (IPS), which examines network traffic flows to detect and prevent vulnerability exploits.

However, such traditional cybersecurity devices have inherent limitations. First, they operate by identifying and mitigating known threats through predefined policies for access control, signatures for byte-level packet inspection and pattern matching, and detection mechanisms for anomalies; as a result, they can only respond reactively to security threats and lack the ability to take proactive measures. Second, they often make false positive (legitimate traffic identified as malicious) and false negative (malicious traffic not detected) predictions. This can lead to legitimate users being blocked or attackers slipping through defenses. Worse yet, each single device can only detect a subset of threats depending on its type, configuration and deployed location. Attackers may devise sophisticated, distributed and coordinated attacks to evade detection, leading to increasing false negative rates.

Overcoming these limitations requires advanced threat intelligence techniques, which gather and analyze information about emerging threats from various sources around the network. Fishing Fort approaches this by means of temporal graph analytics [18]. By integrating event-level threat intelligence feeds from all devices, Fishing Fort can synthesize security events in real-time, effectively discovering vulnerabilities and new attack vectors. It complements hardware-based solutions with a global view over the entire enterprise network.

As an example, consider GAR $\varphi_{9}=Q_{9}[\bar{x}]\left(X_{9} \rightarrow x_{0}\right.$.attack $=\left\langle\right.$ active, $\left.\left.t \in\left[t_{4}, t_{4}+1\right)\right\rangle\right)$ mined from device logs from an enterprise network. It predicts an active attack on subnet $x_{0}$ within the next one min, if the following event series have been reported where consecutive events are at most one min apart from each other: (1) an IPS device detects an Nmap event $\left(x_{1}\right) ;(2)$ a WAF detects a scanner operation $\left(x_{2}\right) ;(3)$ an IPS device reports a Startracker alert $\left(x_{3}\right)$; and (4) an IPS device catches a WannaRen transmission $\left(x_{4}\right)$. This rule has been deployed at a large company, where its accuracy is over $85 \%$. Better still, it allows preemptive defensive measures before the attacks on the subnet are carried out.

## 4 Enriching and Cleaning Graphs

Fishing Fort is also able to enrich (Section 4.1) and clean (Section 4.2) real-life graphs.

### 4.1 Graph Enrichment

It is common to find the data in a real-life graph $G_{1}$ "incomplete", witnessed by missing properties and links. This is because in contrast to relational databases, graph $G_{1}$ is often "schemaless"; in such a graph, entities are specified by vertices and their subgraphs with irregular structures in the absence of constraints. With this comes the need for filling in the information missing from $G_{1}$ with data from external graphs $G_{2}$ that have overlapping information, thereby improving the accuracy of association analyses in graph $G_{1}$.

The need for referencing external graphs has been recognized in medical knowledge discovery [38], which aims to find semantic patterns and improve the accuracy and efficiency of diagnoses and treatment. As reported in [38, 45], as high as $77 \%$ of the discovered patterns span across heterogeneous biological networks. Moreover, e-commerce requires inspecting multiple graphs since an average social media user engages 6.6 different platforms [7]. Analyzing a single platform cannot fully understand users' interests. In addition, recommendation [41], information diffusing prediction [51] and network dynamics analysis [49] have been deducing associations across multiple graphs. Fishing Fort also enriches data for, e.g., drug discovery.

Fishing Fort implements the data enrichment algorithm of [19]. Given a real-life graph $G_{1}$ and an external graph $G_{2}$ with overlapping information, it enriches $G_{1}$ with only relevant information from $G_{2}$, to reduce noise and cost. It develops a graph filtering method to (a) identify vertices $u$ in $G_{1}$ and $v$ in $G_{2}$ that refer to the same real-world entity via heterogeneous entity resolution [15], and (b) locate relevant data of $v$ in $G_{2}$ that pertains to $u$ in $G_{1}$ by training an ML model. It supports two modes: (1) a physical mode by extracting properties of $v$ from $G_{2}$ and enriches $u$ by adding the data to $G_{1}$; and (2) a virtual mode by discovering GARs that pertain to entities in $G_{1}$ across $G_{1}$ and $G_{2}$, without physically merging the two; the discovered GARs are applied to $G_{1}$ and the filtered subgraphs of $G_{2}$, again without merging the two. Fishing Fort supports batch and incremental discovery of such GARs.

For drug discovery, Fishing Fort builds a uniform drug-disease graph by integrating data from eleven libraries and data banks, including CTD [5], MeSH [35] and BioGrid [2]. Given data banks $G_{1}=\left(V_{1}, E_{1}, L_{1}, F_{1}\right)$ and $G_{2}=\left(V_{2}, E_{2}, L_{2}, F_{2}\right)$, Fishing Fort "joins" the two as $G_{\oplus}\left(G_{1}, G_{2}\right)=\left(V_{\oplus}, E_{\oplus}, L_{\oplus}, F_{\oplus}\right)$, where $V_{\oplus}$ (resp. $\left.E_{\oplus}\right)$ is a revision of the union $V_{1} \cup V_{2}$ (resp. $E \cup E_{2}$ ) such that $u$ and $v$ are represented as the same (merged) vertex in $V_{\oplus}$ if $(u, v)$ is a match by parametric simulation [15]; and $L_{\oplus}$ and $F_{\oplus}$ inherit the label and attribute assignments from $G_{1}$ and $G_{2}$. When $u$ and $v$ both carry attribute $A$, the merged vertex takes the value $v . A$ from $G_{i}(\in[1,2])$ if the data in $G_{i}$ is more reliable. It incrementally enriches the graph in the physical mode by extracting data from external sources [19]. Moreover, it cleans the graph by detecting and fixing duplicates and inconsistencies (see Section 4.2).

### 4.2 Graph cleaning

Critical to graph analytics is the quality of the data in graphs. Real-life graphs often have duplicates and conflicts. Even knowledge graphs widely in use include such errors. In Yago, for instance, two different vertices named "Motorola" and "Team Motorola" refer to the same cycling team sponsored by Motorola, yielding a duplicate. The Baron Hirsch Synagogue, a building designed by architect George Awsumb, is labeled as a "flagship" of American Orthodox Judaism, while in DBpedia, this synagogue is classified as a ship. It is known that $26 \%$ of triples in knowledge graph NELL bear conflicts [52], and duplicate entities of Wikidata are involved in $27.8 \%$ factual statements it provides [39]. Moreover, noise in biomedical knowledge graphs is considered a big challenge to drug discovery [50]. Thus, two primitive issues of graph data quality are (a) entity resolution ( $E R$ ), to identify vertices that refer to the same real-world entity, and (b) conflict resolution (CR), to fix inconsistencies among entities. The situation gets worse when it comes to data merged from multiple sources.

Besides ER and CR, there are two other critical issues of data quality. One is timeliness (a.k.a. data currency), for how up-to-date the information is. The other is information completeness, for the availability of data on-hand for analytics. In the real world, data easily becomes obsolete, and stale data is inaccurate. For instance, " $82 \%$ of companies are making decisions based on stale information", and $85 \%$ of the companies witness that "this stale data is leading to incorrect decisions and lost revenue" [3]. Equally damaging is missing data. As revealed by a poll on clinical data management challenges in 2018, $77 \%$ of the participants rated missing patient data as a critical problem [42], which may result in incorrect diagnoses.

Hence the need is evident for (c) timeliness deduction (TD), to deduce temporal orders on attribute values, and (d) missing data imputation (MI), to fill in missing values/links.

One could use GARs to clean graphs. Indeed, GARs can express rules for ER, CR and MI. However, as indicated in Section 2.3, it is intractable to detect and fix errors with GARs. Moreover, GARs stop short of supporting temporal ranking and deducing timeliness.


Figure 3 A graph $G$ of companies and products.

Graph Cleaning Rules. In light of these, Fishing Fort develops a class of rules, referred to as GCRs [12]. A GCR has the form of $\mathcal{Q}\left[x_{0}, y_{0}\right]\left(X \rightarrow p_{0}\right)$. It differs from a GAR in the following.
(1) On the one hand, it adopts a restricted form of graph patterns: $\mathcal{Q}\left[x_{0}, y_{0}\right]$ is a pair $\left\langle Q_{x}\left[x_{0}, \bar{x}\right], Q_{y}\left[y_{0}, \bar{y}\right]\right\rangle$ of patterns, where $Q_{x}$ has a "star" shape centered at a vertex $x_{0}$, which denotes an entity of interest, and links to a set of characteristic features (leaves); similarly for $Q_{y}$. Intuitively, $\mathcal{Q}\left[x_{0}, y_{0}\right]$ represents two entities $x_{0}$ and $y_{0}$ with (possibly) different types and heterogeneous structures in a schemaless graph. It specifies features for pairwise comparison between $x_{0}$ and $y_{0}$. GCRs employ dual star-shaped patterns rather than general (possibly cyclic) patterns in GARs. It is in PTIME to check the matches of such patterns in a graph, as opposed to the intractability of general patterns.
(2) On the other hand, in addition to all the predicates of GARs, GCRs support temporal predicates $x . A \prec y . B$ (resp. $x . A \preceq y . B$ ), indicating that attribute $y . B$ is more current than $x . A$ (resp. at least as current as $x . A$ ). Moreover, Fishing Fort trains a temporal ranking model $\mathcal{M}_{\text {rank }}(x . A, y . B)$, which returns true iff $\mathcal{M}_{\text {rank }}$ predicts that $x . A \preceq y . B$.
(3) GCRs further restrict the preconditions $X$ such that all binary predicates are defined on two leaves $x$ and $y$ in $Q_{x}$ and $Q_{y}$ of $\mathcal{Q}$, respectively, and each leaf may carry at most one such predicate (but multiple unary predicates $z . A \oplus c$ ).

GCRs are able to express rules for ER, CR, TD and MI. As an example, DBpedia and Yago include two company entities having distinct titles "Facebook, Inc." and "Meta Platforms, Inc.", without any timestamp. Worse yet, other data of these entities is either outdated or missing, e.g., revenue, research labs, and type. There are also two products for the online social networking service named "Facebook App". They carry different values for, e.g., current status, version numbers and platforms, but with few timestamps. In fact, snapshot-based knowledge graphs, e.g., DBpedia, maintain the "most recent" facts with no timestamps. Figure 3 depicts such a graph $G$ that includes the product entities $u_{1}, u_{2}$, and companies $v_{1}$, $v_{2}$. To catch errors, we may use the GCRs below with dual patterns in Figure 4.
(1) $\phi_{1}=\mathcal{Q}_{1}\left[x_{0}, y_{0}\right]\left(X_{1} \wedge x_{3}\right.$.val $<y_{3}$.val $\rightarrow x_{3}$.val $\prec y_{3}$.val), where $X_{1}$ is $x_{1}$.id $=y_{1}$.id $\wedge$ $x_{2} \cdot \mathrm{val}=y_{2} \cdot \mathrm{val} \wedge \mathcal{M}_{\text {rank }}\left(x_{4} \cdot \mathrm{val}, y_{4} \cdot \mathrm{val}\right)$. It deduces temporal orders from the version numbers of an online service App (product), i.e., if two services $x_{0}$ and $y_{0}$ are created by the same person, have the same title, and if model $\mathcal{M}_{\text {rank }}$ predicts that $y_{0}$ has newer value for platforms (specified in $X_{1}$ ), then the larger version number of $y_{0}$ is more current (for TD). In practice, the version number of an App grows as the platforms evolve.
(2) $\phi_{2}=\mathcal{Q}_{1}\left[x_{0}, y_{0}\right]\left(X_{1} \wedge x_{3}\right.$.val $\prec y_{3}$.val $\wedge x_{0}$.status $=$ active $\rightarrow y_{0}$.status $=$ active $)$. That is, if service $y_{0}$ has newer values for version numbers (by $x_{3}$.val $\prec y_{3}$.val) than $x_{0}$ and if $x_{0}$ is active, then with the same condition $X_{1}$ as in (1), $y_{0}$ should also be active (for CR).


Figure 4 Example dual patterns.
(3) $\phi_{3}=\mathcal{Q}_{2}\left[x_{0}, y_{0}\right]\left(x_{1}\right.$.id $=y_{1}$.id $\wedge x_{2}$.status $=$ active $\wedge y_{2}$.status $=$ active $\wedge x_{3}$.val $=y_{3}$.val $\wedge$ $x_{4} \cdot \mathrm{val}=y_{5} \cdot \mathrm{val} \rightarrow x_{0}$.id $=y_{0}$.id). It identifies two companies $x_{0}$ and $y_{0}$ (for ER), if they have the same CEO and country of location, and if they own active products of the same title. Here the country property is fetched along different paths in the two stars of $\mathcal{Q}_{2}$.
(4) $\phi_{4}=\mathcal{Q}_{3}\left[x_{0}, y_{0}\right]\left(x_{0}\right.$. type $=$ tech $\wedge y_{0}$.type $=\operatorname{tech} \wedge x_{1}$.id $=y_{1}$.id $\wedge \mathcal{M}_{s}\left(x_{2}\right.$. val, $y_{2}$.val $) \wedge$ $x_{3}$.val $\prec y_{3}, \mathrm{val} \rightarrow x_{4}$.val $\left.\prec y_{4}, \mathrm{val}\right)$. It deduces that company $y_{0}$ has a newer revenue than $x_{0}$ (for TD) if the number of employees of $y_{0}$ is more current, and both $x_{0}$ and $y_{0}$ are tech companies with the same CEO and similar titles (checked by ML model $\mathcal{M}_{s}$ ).
(5) $\phi_{5}=\mathcal{Q}_{4}\left[x_{0}, y_{0}\right]\left(x_{1}\right.$. val $=y_{1}$.val $\wedge \mathcal{M}_{e}\left(x_{2}, y_{2}\right) \wedge x_{3}$.id $=y_{3}$.id $\wedge y_{0}$.CntAILab $=1 \wedge$ $y_{3}$.CntAILab $=1 \rightarrow$ belong_to $\left.\left(x_{2}, x_{3}\right)\right)$. The GCR states that if companies $x_{3}, y_{3}$ and AI labs $x_{2}, y_{2}$ are created by persons $x_{0}$ and $y_{0}$ of the same name, $x_{3}$ and $y_{3}$ are the same entity, $x_{2}$ and $y_{2}$ are identified by an ER model $\mathcal{M}_{e}$, and if $y_{0}$ and $y_{3}$ pertain to AI lab $y_{2}$, then $x_{2}$ is an AI lab belonging to $x_{3}$. It adds a missing link from $x_{2}$ to $x_{3}$ (for MI).

Moreover, Fishing Fort leverages the interaction among ER, CR, TD, and MI to improve the overall quality of the graph. Consider the GCRs above and graph $G$ of Figure 3.
(a) Initially, we deduce that product $u_{2}$ 's version number (427) is more current than the version (30) of $u_{1}$ by using GCR $\phi_{1}$ (TD).
(b) Then a conflict between the status values of products $u_{1}$ and $u_{2}$ is found by GCR $\phi_{2}$, and $u_{2}$ 's status can be rectified to be active (CR).
(c) We next identify companies $v_{1}$ and $v_{2}$ by using GCR $\phi_{3}$ (ER), where pattern nodes $x_{4}$ and $y_{5}$ in $\mathcal{Q}_{2}$ are mapped to vertices with value US.
(d) The type at $v_{1}$ is then copied from (more reliable) $v_{2}$ (MI), as a byproduct of ER.
(e) Next the revenue of $v_{2}$ is verified to be more current than $v_{1}$, via GCR $\phi_{4}$ (TD).
(f) Finally, we deduce a missing link by GCR $\phi_{5}$, i.e., the AI lab $v_{3}$ belongs to $v_{1}$ (MI).

ER, CR, TD and MI help each other. Indeed, ER step (c), CR step (b), TD steps (a) and (e), and MI steps (d) and (f) interact with each other in this process. For instance, step (b) is applicable only after we deduce temporal orders for version numbers in (a); and step (e) needs the results of $E R$ and $M I$ in (c)-(d), which decide the right type value for company $v_{1}$.

Complexity. The restrictions on graph patterns and preconditions make it easier to clean graphs with GCRs. The validation problem becomes tractable for GCRs. Moreover, error detection and correction with GCRs are also in PTIME (see below). One step further, the satisfiability and implication problems are in PTIME if we consider GCRs with predicates $x . A \oplus y . B, x . A \oplus c$ and $\mathcal{M}(x . \bar{A}, y . \bar{B})$ only, where $\oplus$ is either $=$ or $\neq[12]$. These problems become intractable under any of the following conditions, unless $\mathrm{P}=\mathrm{NP}$ : (a) in the presence of link predicates, temporal predicates or comparison $\leq,<, \geq,>$, which are necessary for, e.g., CR, TD, and MI; or (b) if the restrictions on the preconditions $X$ of GCRs are lifted.

Algorithms. Given an (enriched) real-life graph $G$, Fishing Fort discovers a set $\Sigma$ of GCRs and detects and fixes errors with the GCRs using the following algorithms.
(a) Rule discovery [12]. Fishing Fort discovers GCRs from samples of $G$ as remarked earlier [13]. In contrast to how it mines GARs, it makes practical use of star patterns to speed up the discovery process [12]. It computes "scattered matches" of a star pattern, i.e., the matches $\left(h\left(x_{0}\right), h\left(y_{0}\right)\right)$ of the center nodes in $\mathcal{Q}\left[x_{0}, y_{0}\right]$, rather than complete homomorphic matches $h$ of $\mathcal{Q}$. The scattered matches can be computed in PTIME for star patterns via dynamic programming, as opposed to (possibly) exponential time for complete matches of general patterns. As shown in [12], it is much faster to discover GCRs than GARs.
(b) Error detection [12]. Employing the discovered GCRs in $\Sigma$, Fishing Fort detects errors in $G$, i.e., violations of a GCR $\phi=\mathcal{Q}\left[x_{0}, y_{0}\right]\left(X \rightarrow p_{0}\right)$ in $\Sigma$, which are scattered matches $\left(h\left(x_{0}\right), h\left(y_{0}\right)\right)$ for a match $h$ such that $h \models X$ but $h \not \vDash p_{0}$. The violations can be duplicates, conflicts, conflicting timeline or missing links/attributes.
(c) Error correction. Fishing Fort enforces GCRs in $\Sigma$ on graph $G$ via chase [21], to deduce fixes. Besides ER and CR, in the process it determines temporal orders on graph properties, and fills in missing values and links by possibly referencing ground truth $\Gamma$ and knowledge graph KG. It updates $G$ with the deduced fixes, e.g., new edges for missing links. Moreover, it adds the fixes to ground truth $\Gamma$ for subsequent error corrections. The chase is also Church-Rosser, and the fixes are logical consequences of $\Sigma$ and $\Gamma$, i.e., the fixes are validated as long as the GCRs and ground truth are correct. In the process, it suffices to compute scattered matches of patterns, rather than complete ones.
All these algorithms are parallelly scalable and can scale with large graphs in principle. Moreover, the error detection and correction algorithms are in PTIME via scattered matches.

## 5 Conclusion

The novelty of Fishing Fort consists of the following. (1) It makes a first effort to conduct ML prediction and logic deduction in the same process, by embedding ML models as predicates in logic rules. As verified by real-life applications, the unification improves the accuracy of association analyses and the explainability of ML predictions. (2) Fishing Fort automatically discovers rules from real-life graphs, and it supports not only association analyses but also data enrichment and cleaning. (3) It can be readily adapted to different domains and has proven effective in a variety of applications. (4) The algorithms of Fishing Fort are provably parallelly scalable and hence in principle, can scale with large graphs.

We are currently adapting Fishing Fort to quantitative trading, fraud detection, and manufacturing industry beyond EV batteries. The preliminary results are quite encouraging.

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