

# Pure Methods for roDOT (Artifact)

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## Abstract

The artifact for the paper Pure methods for roDOT (ECOOP 2024) contains the Coq mechanization of the theorems appearing in the paper, and the necessary definitions and lemmata. Additionally, the artifact contains a mechanization of the roDOT calculus presented in an earlier paper Reference mutability for DOT (ECOOP 2020). We used the

calculus from this paper as the baseline for our paper, but it has not been mechanized before.

The functionality of the artifact is the ability to verify the correctness of the theorems by running Coq.

Our code is based on a mechanization of a soundness proof for Field Mutable DOT.

**2012 ACM Subject Classification** Software and its engineering → Formal language definitions; Software and its engineering → Object oriented languages

**Keywords and phrases** type systems, DOT calculus, pure methods

**Digital Object Identifier** 10.4230/DARTS.10.2.6

**Funding** This work was supported by the Czech Science Foundation project 23-06506S, and by the Czech Ministry of Education, Youth and Sports project LL2325 of the ERC.CZ programme. This research was also supported by the Natural Sciences and Engineering Research Council of Canada.

**Related Article** Vlastimil Dort, Yufeng Li, Ondřej Lhoták, and Pavel Parížek, “Pure Methods for roDOT”, in 38th European Conference on Object-Oriented Programming (ECOOP 2024), LIPIcs, Vol. 313, pp. 13:1–13:29, 2024.

<https://doi.org/10.4230/LIPIcs.ECOOP.2024.13>

**Related Conference** 38th European Conference on Object-Oriented Programming (ECOOP 2024), September 16–20, 2024, Vienna, Austria

**Evaluation Policy** The artifact has been evaluated as described in the ECOOP 2024 Call for Artifacts and the ACM Artifact Review and Badging Policy.

## 1 Scope

The Coq code contains mechanizations of the theorems and the necessary definitions and lemmata in the submitted paper and its extended version [2]. Additionally, the artifact contains a mechanization of the roDOT calculus presented in the paper Reference mutability for DOT [1]. The code is based on a mechanization of soundness proof for Field Mutable DOT [3].

### ■ Figure 1

- **Variables** – The mechanization uses a *locally nameless representation of variables*, see definition `avar` in `Syntax/Vars.v`. The kinds of variables (location, reference, parameter) are defined as `varkind` in `Syntax/Vars.v`. We use the typing context to associate the kind with a variable.
- **Terms** are defined as `trm` and `lit` in `Syntax/Terms.v`.



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Dagstuhl Artifacts Series, Vol. 10, Issue 2, Artifact No. 6, pp. 6:1–6:8



DAGSTUHL  
ARTIFACTS SERIES

Dagstuhl Artifacts Series

Schloss Dagstuhl – Leibniz-Zentrum für Informatik,  
Dagstuhl Publishing, Germany



## 6:2 Pure Methods for roDOT (Artifact)

- **Definitions** are defined as `def` and `defs` in `Syntax/Terms.v`.
- **Stack** is defined as `stack` in `Syntax/Stack.v`.
- **Types** are defined as `typ` and `dec` in `Syntax/Types.v`.
- **Type names** are defined as `typ_label` in `Syntax/Labels.v`.
- **Heap** is defined as `heap` in `Syntax/Heap.v`.
- **Configuration** is defined as `config` in `Syntax/AbstractMachine.v`.
- **Environment** is defined as `renv` in `Syntax/Env.v`.
- Figure 2 contains selected rules from Figures 8 and 10 in the appendix – see the corresponding entries.
- **Figure 3** – Mutable reachability (Rea) is defined as `mut_reach` in `Mutability/MutableReachability.v`.
- **Theorem 1** – `soundness_initial` in `Safety.v`
- **Theorem 2** – `immutability_guarantee` in `Mutability/ImmutabilityGuarantee.v`.
- Definition 8 does not have a direct counterpart in the Coq code, subtyping is defined by `subtyp` in `GeneralTyping/GeneralTyping.v`.
- **Lemma 9** – `reference_nocap_type` in `CanonicalForms/ReferenceTypes.v`.
- Definition 11 does not have a direct counterpart in the Coq code. It is used unfolded in the premises of Theorem 16 and Definition 26.
- **Figure 4**
  - **The first rule** (TS-N) is defined as `ty_incap_nocap` in `GeneralTyping/GeneralTyping.v`.
  - **The second rule** (ST-NM) is defined as `subtyp_nocap_mut_top_boundless` in `GeneralTyping/GeneralTyping.v`.
- **Figure 5**
  - **General subtyping** is defined as `subtyp` in `GeneralTyping/GeneralTyping.v`.
  - **Tight subtyping** is defined as `subtyp_t` in `CanonicalForms/TightTyping.v`.
  - **Precise typing** is defined using `precise_flow` in `CanonicalForms/PreciseTyping.v`.
  - **General typing** is defined as `ty_var` in `GeneralTyping/GeneralTyping.v`.
  - **Tight typing** is defined as `ty_trm_t` in `CanonicalForms/TightTyping.v`.
  - **Invertible typing** is defined as `ty_var_inv` in `CanonicalForms/FlatInvertibleTyping.v`.
- **Lemma 12** – `ty_incap_nocap` and `ty_incap_diag_nocap_sup` in `GeneralTyping/GeneralTyping.v`.
- **Lemma 13** – `invertible_flat_typing_closure_tight` in `CanonicalForms/FlatInvertibleTyping.v`.
- **Lemma 14** – `invertible_flat_typing_or_inv` in `CanonicalForms/FlatInvertibleTyping.v`.
- Figure 7 contains selected rules from Figures 18 and 19 in appendix – see the corresponding entries.
- Definition 15 does not have a direct counterpart in the Coq code. It is used unfolded in the conclusion of Theorem 16.
- **Theorem 16** – `SefG_I` in `Mutability/SefGuarantee.v`
- **Lemma 17** – `imm_transport` in `Mutability/SefGuarantee.v`
- **Lemma 18** – `sef_neq_elim_ty_hole` and `sef_neq_elim_heap_corr` in `Mutability/SefGuarantee.v`
- **Lemma 19** – `sef_neq_ro_ty_config` in `Mutability/SefGuarantee.v`
- **Lemma 20** – `ref_elim_similar_conf_sef` in `Similarity/ConfigSefSimilarity.v`
- **Definition 21** – `heap_flds_sim` in `Mutability/SefGuarantee.v`
- **Lemma 22** – `red_heap_flds_sim` in `Mutability/SefGuarantee.v`

- **Definition 23** – Transform in Transformation/Transformation.v
- Definition 24 does not have a direct counterpart in the Coq code. It is used unfolded in the conclusions of Theorem 25 and Lemma 58. The similarity transformation is defined as trf\_similarity in Transformation/TransformationSimilarity.v.
- **Theorem 25** – transformation\_preserved\_if\_terminates in Transformation/TransformationLiftingPreservation.v
- **Definition 26** – trf\_swap\_calls\_local in Transformation/TransformationSwapCalls.v
- **Theorem 27** – swap\_calls\_transformation\_guarantee in Transformation/TransformationSwapCallsGuarantee.v
- **Figure 8** – ty\_trm in GeneralTyping/GeneralTyping.v
- **Figure 9** – ty\_var in GeneralTyping/GeneralTyping.v
- **Figure 10** – subtype in GeneralTyping/GeneralTyping.v
- **Figure 11** – ty\_incap and typ\_capbnd in GeneralTyping/GeneralTyping.v
- **Figure 12** – ty\_def and ty\_defs in GeneralTyping/GeneralTyping.v
- **Figure 13** – red in OperationalSemantics/OperationalSemantics.v
- **Figure 14**
  - **Heap correspondence** is defined as heap\_correspond in CanonicalForms/HeapCorrespondence.v.
  - **Environment correspondence** is defined as renv\_corr in CanonicalForms/EnvCorrespondence.v.
  - **Stack typing** is defined as ty\_stack in CanonicalForms/ConfigTyping.v.
  - **Configuration typing** is defined as ty\_config in CanonicalForms/ConfigTyping.v. This definition has several assumptions about well formedness of the configuration (using variables of the correct kind and no unbound variables).
- **Figure 15** – ty\_inv\_atomic in CanonicalForms/LayeredTyping/LayeredTypingAtomic.v.
- **Figure 16** – ty\_inv\_basic in CanonicalForms/LayeredTyping/LayeredTypingBasic.v.
- **Figure 17** – ty\_inv\_basic\_closure in CanonicalForms/LayeredTyping/LayeredTypingBasicClosure.v.
- **Figure 18** – ty\_inv\_logic in CanonicalForms/LayeredTyping/LayeredTypingLogic.v.
- **Figure 19** – ty\_inv\_main in CanonicalForms/LayeredTyping/LayeredTypingMain.v.
- **Figure 20** – subtype\_atomic in CanonicalForms/LayeredTyping/LayeredSubtypingAtomic.v.
- **Figure 21** – ty\_has\_M and ty\_has\_N\_atomic in CanonicalForms/LayeredTyping/LayeredCapabilityBasic.v.
- **Figure 22** – ty\_has\_M\_closure and ty\_has\_N\_closure in CanonicalForms/LayeredTyping/LayeredCapabilityBasicClosure.v.
- **Lemma 28** – invertible\_main\_to\_precise\_typ\_dec in CanonicalForms/LayeredTyping/LayeredTypingMainHard.v.
- **Lemma 29** – invertible\_main\_to\_precise\_fld\_dec in CanonicalForms/InvertibleTyping.v.
- **Lemma 30** – invertible\_main\_to\_precise\_met\_dec in CanonicalForms/LayeredTyping/LayeredTypingMainHard.v.

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- **Lemma 31** – `tight_to_invertible_main` in `CanonicalForms/LayeredTyping/LayeredTypingMainHard.v`.
- **Lemma 32** – `invertible_main_typing_closure_tight` in `CanonicalForms/LayeredTyping/LayeredTypingMainHard.v`.
- **Lemma 33** – `ty_inv_main_lc_and` in `CanonicalForms/LayeredTyping/LayeredTypingMainHard.v`.
- **Lemma 34** – `ty_inv_main_lc_and_invl` and `ty_inv_main_lc_and_invr` in `CanonicalForms/LayeredTyping/LayeredTypingMain.v`.
- **Lemma 35** – `ty_inv_main_lc_or_diag` in `CanonicalForms/LayeredTyping/LayeredTypingMainHard.v`.
- **Lemma 36** – `ty_inv_main_lc_nocap_main_replace` in `CanonicalForms/LayeredTyping/LayeredTypingMain.v`.
- **Lemma 37** – `ty_inv_main_tight` in `CanonicalForms/LayeredTyping/LayeredTypingMainCount.v`.
- **Lemma 38** – `ty_inv_main_lc_N_cases` in `CanonicalForms/LayeredTyping/LayeredTypingMainHard.v`.
- Definitions 39 to 43 do not have a conterpart in the Coq code.
- **Definition 44** – We use a pair of lists of variables (`list var`).
- **Definition 45** – `similar_trm`, `similar_avar`, `similar_item`, and `similar_stack` in `Similarity/SyntaxSimilarity.v`
- **Definition 46** – `similar_conf_sef` in `Similarity/ConfigSefSimilarity.v`
- **Lemma 47** – `conf_sim_red_append` in `Similarity/ConfigSefSimilarity.v`
- **Lemma 48** – `conf_sim_red_create` in `Similarity/ConfigSefSimilarity.v`
- **Definition 49** – `TransformCondTypeIdentical` in `Transformation/Transformation.v`, applied using `TransformEnsures`
- **Definition 50** – `TransformCondTyping` in `Transformation/TransformationTerm.v`, applied using `TransformRequires`
- **Figure 23** – `trf_local_idtyp_trm`, `trf_local_idtyp_lit`, `trf_local_idtyp_def`, and `trf_local_idtyp_defs` in `Transformation/TransformationLifting.v`
- **Figure 24** – `trf_focus_idtyp_conf` and `trf_lift_idtyp_conf` in `Transformation/TransformationConfig.v`
- **Definition 52** – `TransformWeakeningCompat` in `Transformation/TransformationTerm.v`
- **Lemma 53** – `WeakeningCompatTransformationTrm` in `Transformation/TransformationLifting.v`
- **Definition 54** – Expressed by composing `TransformPreserves` in `Transformation/Transformation.v` with `TransformIsAnswer` in `Transformation/TransformationConfig.v`
- **Lemma 55** – `transformation_preserved` in `Transformation/TransformationLiftingPreservation.v`
- **Definition 56** – `TransformConfigReducesToShortIfTerminates` in `Transformation/TransformationConfig.v`, applied to `trf_similarity` in `Transformation/TransformationSimilarity.v`.
- **Lemma 57** – `TransformConfigReducesTo1Similarity` in `Transformation/TransformationSimilarity.v`,
- **Lemma 58** – `swap_calls_transformation_preservation` in `Transformation/TransformationSwapCallsGuarantee.v`
- **Lemma 59** – `TransformSwapCallsWeakening` in `Transformation/TransformationSwapCalls.v`
- **Lemma 60** – `transformation_swap_calls_reduces_to_similarity` in `Transformation/TransformationSwapCallsPreservation.v`

## 2 Content

The artifact package includes:

- The main component of the artifact is a **Coq project** containing the definitions of the type system in the paper and proofs of its soundness and the guarantees. The project contains the **Coq source code**. In the provided Docker image, the source code can be found under the directory `/root/rodot`.

## 3 Getting the artifact

The artifact endorsed by the Artifact Evaluation Committee is available free of charge on the Dagstuhl Research Online Publication Server (DROPS). In addition, the artifact is also available at: <https://hub.docker.com/r/rodotcalculus/ecoop2024-artifact>.

## 4 Tested platforms

Running the artifact requires an **x86\_64** machine with **Linux** and **Docker**.

## 5 License

The artifact is available under the MIT license.

## 6 MD5 sum of the artifact

a32d393a3275275c52e0ae40115360c6

## 7 Size of the artifact

677.5 KiB

## A Building the project

Compiling the code requires Coq<sup>1</sup> version 8.10.2, and the TLC library<sup>2</sup> version 20181116.

The following commands can be used to install Coq and TLC using the OCaml Package Manager<sup>3</sup>:

```
opam init --compiler=4.09.1 --disable-sandboxing -a
opam pin add coq 8.10.2 -y
opam repo add coq-released http://coq.inria.fr/opam/released
opam pin add coq-tlc 20181116 -y
```

To build the project and verify the correctness of the proof, run the following command in the `rodot` directory of the artifact:

```
make -j4
```

<sup>1</sup> <https://coq.inria.fr/>

<sup>2</sup> <https://www.chargueraud.org/softs/tlc/>

<sup>3</sup> <https://opam.ocaml.org/>, <https://coq.inria.fr/opam-using.html>

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### B Quick-start guide for the Docker image

1. **Run the docker image.** To run the Docker image on your Linux machine, execute the following command.

```
sudo docker run -it --rm rodotcalculus/ecoop2024-artifact
```

2. **Find the source code.** When you run the docker image, a shell will start in the directory `/root/rodot`. The `*.v` files in this directory and its subdirectories constitute the source code.
3. **Build the project.** To build the project and verify the correctness of the proof, run `make -j4`. You can omit the `-j4` option or use a different number to control the level of parallelism of the build.

### C Re-creating the Docker image locally

The docker image can also be re-created locally from the artifact source code and the provided Dockerfile, using the following command:

```
sudo docker build -t ecoop2024-artifact .
```

### D Typing modes

Our Coq definitions and theorems support extensibility, which allows extending the calculus with additional typing rules, and verifying multiple versions of the calculus simultaneously. This is achieved by parameterizing the definitions and theorems with the parameter `typing_mode`. Possible values of `typing_mode` are defined in `GeneralTyping/TypingMode.v`. Each value represent a version of the calculus, where each version can have a different set of features. Some typing rules and theorems are only available if a specific feature is enabled. This is achieved by a feature check in the rule or theorem, for example `mode_has_mutability typing_mode ->`.

- For the mechanization of the related paper, the mode representing this version of the calculus is `rodot_sef`.
- For the mechanization of [1], the mode representing this version of the calculus is `rodot`.

### E Differences between the paper presentation and mechanization

There are several differences between the presentation in the paper and the mechanization, in order to improve readability of the paper and improve organization and extensibility of the code.

- The mechanized syntax uses a locally nameless representation, where variables bound in terms and literals are represented by deBruijn indices rather than variable names.
- Definitions of an object are represented by a list of definitions (while they are structured by a binary intersection in the paper definition, the structure is irrelevant).
- The mechanization represents multiple variants of the calculus, where the syntax is shared, but the differences in typing rules are achieved through the typing mode mechanism described above.
- The mechanized syntax contains additional constructors that are not part of roDOT, such as `trm_apply`, `lit_fun`, `ctx_stop`, `item_fun`. However, the typing rules related to these constructors are disabled by the typing mode feature checks explained above. Since the theorems involve typed terms and machine configurations, these additional constructors are irrelevant.

- The kind of a variable (reference/location, etc.), which is determined by the variable letter in the paper, is kept track of in the typing context in the mechanization.
- The special handling of the self-reference in the typing of object literals and objects on the heap is implemented using the `objctx` parameter of typing. This is a parameter of each typing judgment in addition to the usual typing context. This allows typing object literals and objects on the heap with the same typing rules, passing `objctx_lit` for typing object literals and `objctx_heap` for typing heap items. For term typing, the `objctx` is empty.
- To avoid conflicts of variable names, the mechanized definitions and theorems contain additional well-formedness and freshness premises where necessary. These premises are implicitly assumed and not shown in the paper version.
- For the purpose of generating fresh variables and ensuring no conflict of variable names between entries of the machine configuration and types in the typing context, machine configurations carry an additional entry `Lv`, which stores all the variable names that appeared at any step of the execution so far.
- Definition types and object literals are not part of the definition of terms (`trm`) and types (`typ`) directly, but use separate definitions (`lit`, `def`) used through constructors `typ_rcd`, `lit_obj`.
- We use additional definitions to avoid code repetition and to improve extensibility.
- The definitions of transformations and similarity are structured using the type classes feature of Coq, to allow reusing definitions and lemmas for different syntactic elements.

## F Checking theorem assumptions

Coq code can use additional axioms, which are assumed true, so the correctness of the evaluation depends on correctness of the used axioms.

This artifact uses the following axioms of classical logic:

```
LibAxioms.prop_ext (from TLC library)
LibAxioms.indefinite_description (from TLC library)
LibAxioms.fun_ext_dep (from TLC library)
Classical_Prop.classic
```

In order to check what axioms are used (and that no additional axioms are used), we provide the script `print-assumptions.sh`. Its first argument names a module, and its second argument names a theorem to check.

To check the axioms used by the main theorems, run the following commands **after building the project**:

```
./print-assumptions.sh Safety soundness_initial
./print-assumptions.sh \
  Mutability.ImmutabilityGuarantee immutability_guarantee
./print-assumptions.sh Mutability.SefGuarantee SefG_I
./print-assumptions.sh \
  Transformation.TransformationSwapCallsGuarantee \
  swap_calls_transformation_guarantee
```

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References

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- 1 Vlastimil Dort and Ondřej Lhoták. Reference mutability for DOT. In Robert Hirschfeld and Tobias Pape, editors, *34th European Conference on Object-Oriented Programming, ECOOP 2020, November 15-17, 2020, Berlin, Germany (Virtual Conference)*, volume 166 of *LIPICs*, pages 18:1–18:28. Schloss Dagstuhl – Leibniz-Zentrum für Informatik, 2020. doi:10.4230/LIPICs.ECOOP.2020.18.
- 2 Vlastimil Dort, Yufeng Li, Ondřej Lhoták, and Pavel Parížek. Pure methods for ro-DOT (an extended version). Technical Report D3S-TR-2024-01, Dep. of Distributed and Dependable Systems, Charles University, 2024. URL: [https://d3s.mff.cuni.cz/files/publications/dort\\_pure\\_report\\_2024.pdf](https://d3s.mff.cuni.cz/files/publications/dort_pure_report_2024.pdf).
- 3 Ifaz Kabir. themaplelab/dot-public: A simpler syntactic soundness proof for dependent object types. <https://github.com/themaplelab/dot-public/tree/master/dot-simpler>.